

Thermodynamics

Formulae

to remember.

1st law:

$$du = dq + dw$$

↑
internal energy change
of system

↑
heat input
to system

work done on
system

U is a state function

q, w are path functions

$$du = c_v dt$$

$$dw = -pdv$$

$$\left[c_v = \frac{\partial q}{\partial T} \right]_v$$

Entropy

$$ds = dq_{rev} / T$$

S is a state function

⇒ rewrite 1st law:

$$c_v dt = T ds - pdv$$

Also:

$$c_p = \left. \frac{\partial q}{\partial T} \right|_p$$

⇒ for ideal gas (PV = nRT)

$$c_p = c_v + R_n$$

pick reversible
paths

Carnot cycle is reversible and most efficient heat cycle.

$$\text{Efficiency (general)} = \eta = \frac{W}{Q_1}$$

$$= 1 - \frac{T_2}{T_1} \text{ for Carnot cycle.}$$

A-B: Isothermal expansion @ T_1

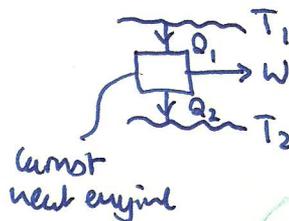
B-C: Adiabatic expansion

C-D: Isothermal compression

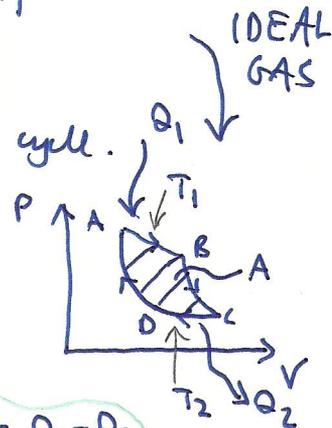
D-A: Adiabatic compression

$$\begin{cases} PV^\gamma = \text{constant} \\ p \cdot \gamma \cdot T = \text{constant} \\ TV^{\gamma-1} = \text{constant} \end{cases}$$

Find Q_1, Q_2
in terms of T_1, T_2
only. Then find $\eta = \frac{Q_1 - Q_2}{Q_1}$



Carnot
heat engine



$$W_{net} = Q_1 - Q_2$$

$$= \int_A \text{d}P dV$$

No du
overall in
process A→A.

Kelvin's Statement:

"No process whose sole purpose is heat → work" ↓

Clausius "

"No process can transfer heat from hot to cold body"

2nd law:

$$dS_{universe} \geq 0 \text{ for any spontaneous process.}$$