

- (a) A chain of resistors, Figure 1.a.i, is composed of n units, each consisting of three resistors, each resistor of resistance R , Figure 1.a.ii. A unit is attached to the left hand end of the chain in order to increase the number of units from n to $(n+1)$.

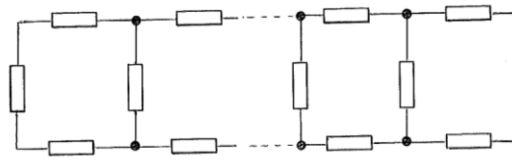


Figure 1.a.i

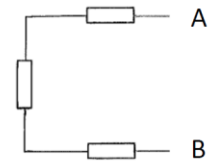


Figure 1.a.ii

- (i) Calculate the resistance (between A and B) across a chain with two units, R_2 , and the resistance R_3 , across a chain with three units.
- (ii) A unit is attached to a long chain. The resistance of the chain, R_T , is not altered by this addition. Determine the resistance of the chain.

[6]

(b)

- (i) A satellite is in orbit just above a spherical planet of radius R and uniform density ρ . If the periodic time for each orbit is T , find an expression for ρT^2 . Comment on the result.
- (ii) A man with a mass of 75 kg stands at the end of a diving board, depressing it by 0.30 m. What would be the period of his motion if he was to jump lightly in rhythm with the harmonic motion of the diving board?

[6]

(c)

- (i) A uniform vertical tube, open at the lower end and sealed at the upper end, is lowered into sea water, trapping air in the tube. When the tube is submerged to a depth of 10.0 m, sea water has exactly filled the lower half of the tube. To what depth must the tube be lowered so that sea water fills 90% of the tube?
- (ii) A mercury barometer has some air above the mercury, Figure 1.c.i. The top of the barometer is 1.000 m above the level of the mercury in the reservoir. When the tube is vertical the height of the mercury column is 0.700 m. When the tube is inclined at 60° to the vertical, Figure 1.c.ii, the reading of the mercury level is 0.950 m. What is the atmospheric pressure in mm of mercury?

[6]

Figure 1.c.i

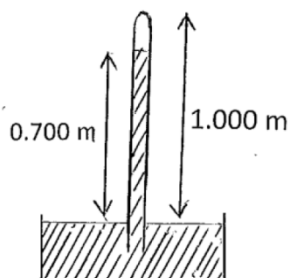
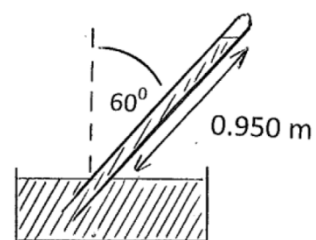


Figure 1.c.ii



- (d) A car travels along a horizontal road starting at time $t = 0$, and finishing at $t = \pi/10$. At time t it has travelled a distance x , has a speed v and an acceleration f given by
- $$x = A \sin(5t), \quad v = 5A \cos(5t) \quad \text{and} \quad f = -25A \sin(5t), \quad \text{where } A \text{ is a constant.}$$

Determine the average speed, v_{AV} , and average acceleration, f_{AV} .

[3]

- (e) One gram of hydrogen atoms is separated into electrons and protons. The electrons are deposited on the Moon, the protons remaining on the Earth. What, numerically, is the force that results? The Earth – Moon distance is $R_{EM} = 3.84 \times 10^8$ m.

[5]

- (f) Determine the half life of uranium given that 3.23×10^{-7} g of radium is found per gram of uranium in ancient minerals. The half life of radium is 1,600 years. The atomic weights of uranium and radium are 238 and 226 respectively. All the radium arises from the uranium.

[5]

- (g) A mixed beam of deuterons (an isotope of hydrogen, ${}^2\text{H}^+$) and protons, which have been accelerated through $1.00 \times 10^4 \text{ V}$, enter a uniform magnetic field of 0.500 T in a direction at right angles to the field. Calculate the separation of the proton beam from the deuteron beam when each has described a semicircle in the field.

[6]

- (h) A sound source, frequency f and velocity u , is moving along a straight line towards an observer who is approaching the sound source with velocity v . Determine the frequency f_o heard by the observer if the speed of sound is c .

A moving sound source, S, has velocity of 15.0 m s^{-1} and frequency 200 Hz . An observer P, speed 18.0 m s^{-1} , and S are approaching a point Q along paths inclined at 30° to each other, Figure 1.h. What frequency is heard by the observer when S and P are equidistant from Q? The speed of sound is 331 m s^{-1} .

[8]

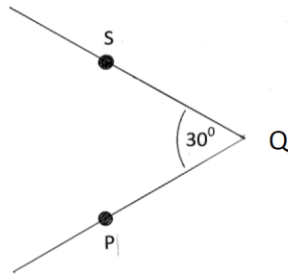


Figure 1.h

- (i) A beaker, containing some water, has a total mass of 0.300 kg. The beaker rests on a weighing scale. A 250 g copper sphere, density $8.93 \times 10^3 \text{ kg m}^{-3}$, is suspended so that it is completely immersed in the water, but does not touch the bottom of the beaker. What is the reading on the weighing scale in newtons? The density of water is $1.00 \times 10^3 \text{ kg m}^{-3}$.

[3]

- (j) A capacitor, capacitance C_1 , with a charge Q_0 , is connected in a closed (loop) series circuit with an uncharged capacitor, capacitance C_2 and a switch, which is initially open. Compare the energy stored in the capacitors before and after the switch is closed by considering the potential across each capacitor. What can one conclude?

[8]

(k)

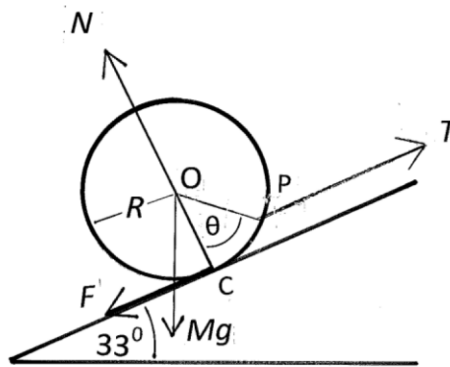


Figure 1.k

A uniform sphere, radius R and mass $M = 5.00$ kg, is pulled up an inclined plane, inclination 33.0° to the horizontal, by a string of tension T , which is attached to a point P on its surface, making an angle θ with the line joining the centre of the sphere, O , and its contact point with the plane, C . The string is parallel to the plane. The coefficient of friction between the sphere and the plane $\mu = 0.420$. The sphere is about to slide up the plane. The frictional force is F and the normal reaction is N , Figure 1.k.

Determine, numerically:

- (i) T , by resolving the forces along and perpendicular to the slope
- (ii) θ .

[10]

- (I) Three boats start at time $t = 0$ from the corners of an equilateral triangle, of side 50 km, and maintain constant speeds of 30 km hr^{-1} during the subsequent motion. They each maintain a heading, clockwise, towards the neighbouring boat. They all eventually meet at P.

Determine:

- (i) qualitatively, the evolution of the triangle formed by the three boats
- (ii) the velocity components of the three boats in the direction of P, as a function of time, t , and in the perpendicular directions
- (iii) the time, t_M , at which they all meet
- (iv) the distance travelled by each boat, D .

[8]

- (m) A bicycle tyre has a volume of $1.20 \times 10^{-3} \text{ m}^3$ when fully inflated. The barrel of the bicycle pump has a working volume of $9.0 \times 10^{-5} \text{ m}^3$. How many strokes of the pump are needed to completely inflate the flat tyre to a total pressure of $3.0 \times 10^5 \text{ Pa}$? The atmospheric pressure is $1.00 \times 10^5 \text{ Pa}$. Assume the air is pumped in slowly, so that the temperature remains constant.

[4]