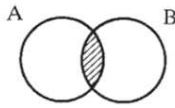
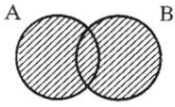


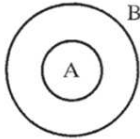
1.  $\cap$  'intersection'  
 $A \cap B$  is shaded.



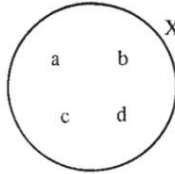
2.  $\cup$  'union'  
 $A \cup B$  is shaded.



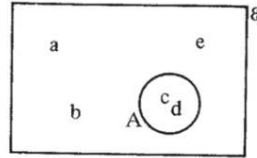
3.  $\subset$  'is a subset of'  
 $A \subset B$   
 [ $B \not\subset A$  means 'B is not a subset of A']



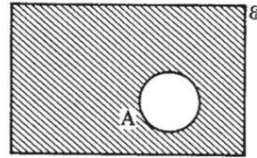
4.  $\in$  'is a member of'  
 'belongs to'  
 $b \in X$   
 [ $e \notin X$  means 'e is not a member of set X']



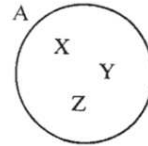
5.  $\mathcal{E}$  'universal set'  
 $\mathcal{E} = \{a, b, c, d, e\}$



6.  $A'$  'complement of'  
 'not in A'  
 $A'$  is shaded  
 ( $A \cup A' = \mathcal{E}$ )



7.  $n(A)$  'the number of elements in set A'  
 $n(A) = 3$

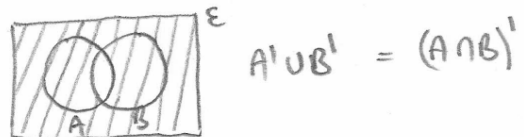
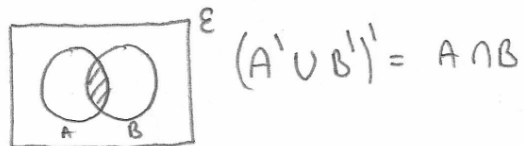
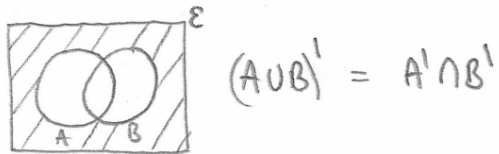


8.  $A = \{x : x \text{ is an integer, } 2 \leq x \leq 9\}$

The **set of** elements  $x$  **such that**  $x$  is an integer and  $2 \leq x \leq 9$ .  
 The set A is  $\{2, 3, 4, 5, 6, 7, 8, 9\}$ .

9.  $\emptyset$  or  $\{\}$  'empty set'  
 (Note  $\emptyset \subset A$  for any set A)

# Rules and notation of mathematical logic

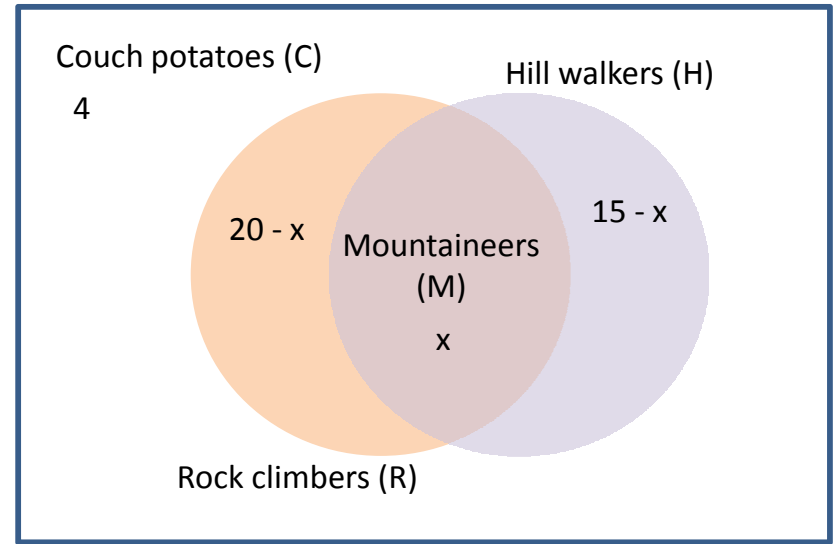


**George Boole**  
 1815-1864

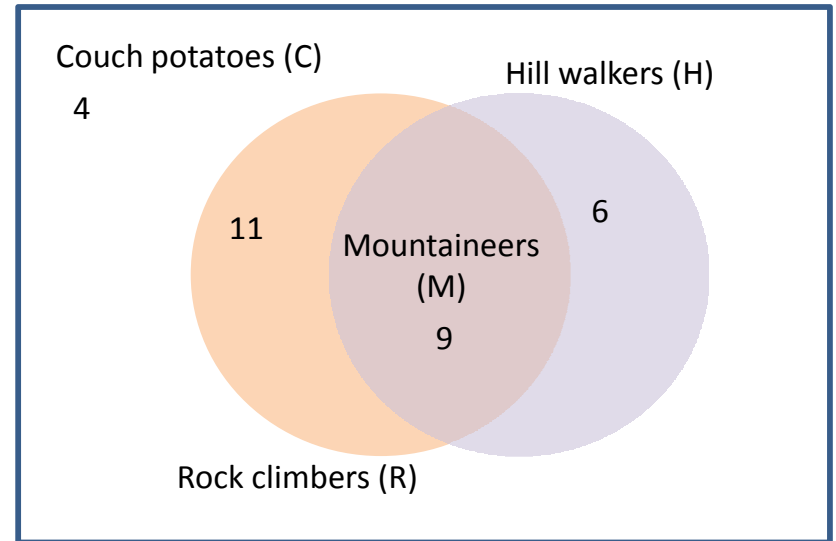
## Boolean algebra

- $A \cap (B \cup C) = (A \cap B) \cup (A \cap C)$
- $A \cup (B \cap C) = (A \cup B) \cap (A \cup C)$
- $A \cap (A \cup B) = A$
- $A \cup (A \cap B) = A$
- $A' \cap B' = (A \cup B)'$
- $A' \cup B' = (A \cap B)'$

Last two are the *De-Morgan laws*



30 attendees at the local BMC meeting. 20 rock climbers and 15 hill walker + 4 couch potatoes. How many mountaineers?  
 $4 + 20 - x + x + 15 - x = 30$   
 Hence  $39 - x = 30 \Rightarrow x = 9$  mountaineers



$n(M) = 9$ ;  $n(R) = 20$ ;  $n(R \cup H) = 26$ ;  $n(\mathcal{E}) = 30$