

# FORCES + MOTION REVISION NOTES

## VECTOR + SCALAR QUANTITIES

SCALAR QUANTITY has only magnitude or size only

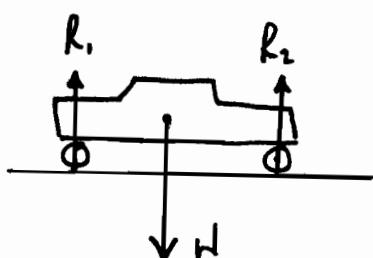
e.g. mass, energy, distance, speed, temperature

VECTOR QUANTITY has both magnitude + direction

e.g. velocity, acceleration, force, displacement, weight

Vector quantities are often represented as arrows, where the length represents the magnitude of the vector and the direction is shown by the arrow head

e.g.



$W$  = weight of car

$R_1 + R_2$  = Normal reaction forces.

MASS (kg) - Property of a body that is irrespective of location. e.g. a man has a mass of 70kg both on the Earth and on the Moon.

WEIGHT (N) - The weight of an object depends on both the mass and the location of the object:  
gravitational field strength

$$\text{Weight} = \text{Mass} \times \text{Gravitational Field Strength}.$$

$$\text{Weight} = M \times g$$

$$N = kg \times N/kg$$

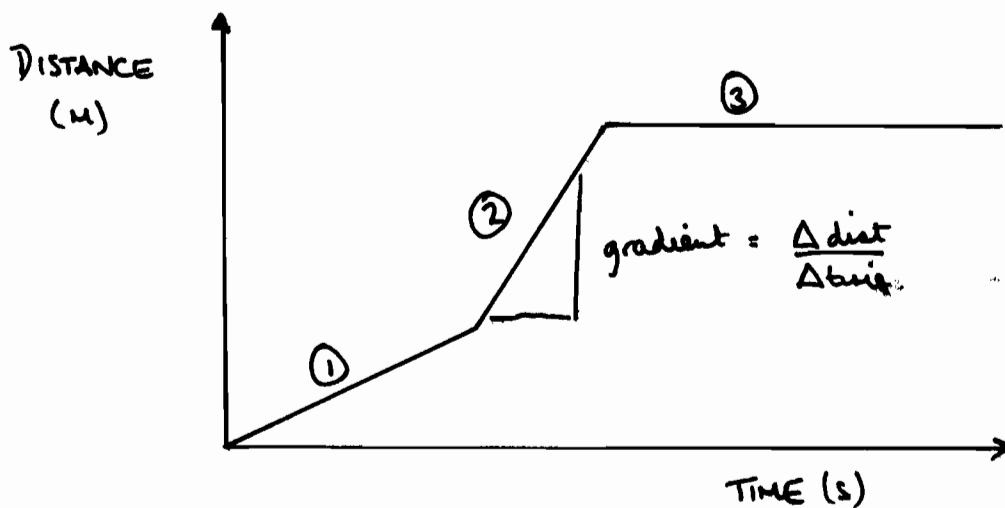
Earth's Gravitational Field Strength,  $g_e = 10 \text{ N/kg}$  (unless specified otherwise)  
in GCSE papers

Moon Gravitational Field Strength,  $g_{\text{moon}} = 1.6 \text{ N/kg}$

$$\therefore \text{Weight of man of mass } 70\text{kg on Earth} = M \times g = 70 \times 10 = \underline{700\text{N}}$$

$$\text{on Moon} = M \times g_{\text{moon}} = 70 \times 1.6 = \underline{112\text{N}}$$

## DISTANCE - TIME GRAPHS

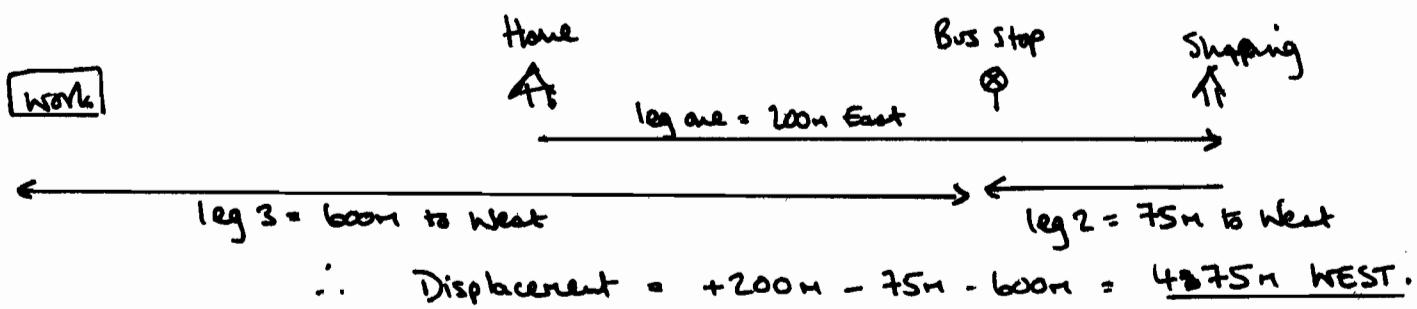


- Graph shows how the distance travelled by an object changes over time.
- The gradient of the graph  $\Rightarrow$  gradient =  $\frac{\Delta \text{distance}}{\Delta \text{time}} = \text{Speed}$
- ∴ ①  $\Rightarrow$  object moving at a constant speed. (... gradient).
- ②  $\Rightarrow$  object increases its speed. (steeper gradient).
- ③  $\Rightarrow$  object stationary (gradient = 0).

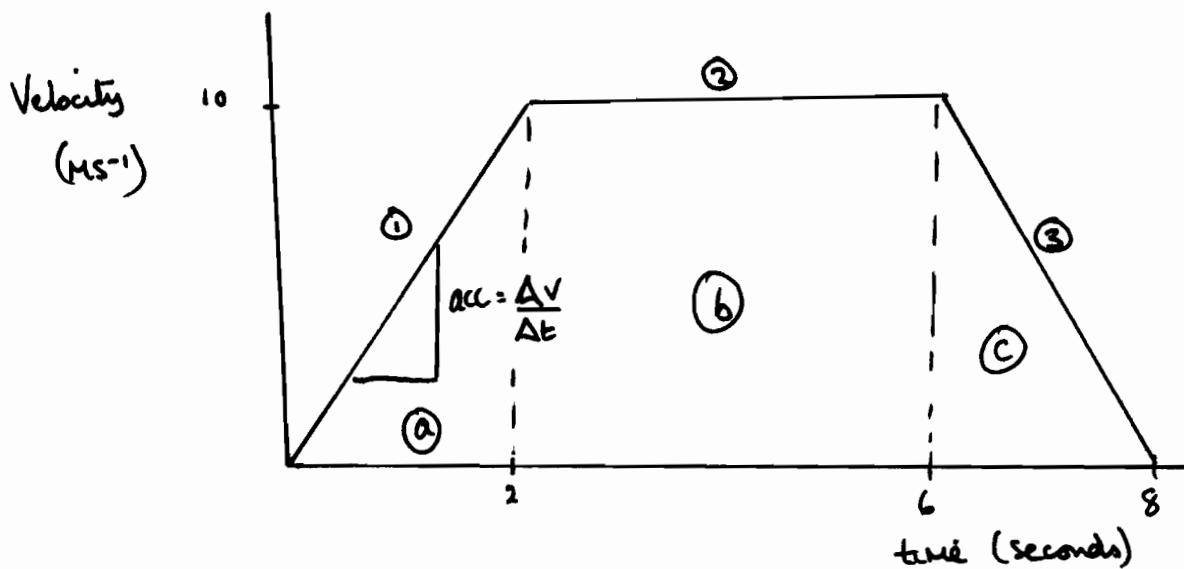
## SPEED, DISTANCE, TIME RELATIONSHIP

- The gradient of the above graph  $\Rightarrow$  Speed =  $\frac{\Delta \text{distance} (\text{m})}{\Delta \text{time} (\text{s})}$
- Speed is measured in m/s or  $\text{ms}^{-1}$
- Speed is a scalar quantity  $\therefore$  no defined direction. Velocity is speed in a specific direction.
- Distance is a scalar quantity, whilst displacement is the vector equivalent.

**DISPLACEMENT:** Mark starts at home and makes a journey to the shop, the bus stop and then work : what is his displacement



## VELOCITY-TIME GRAPHS.



- Velocity-Time graphs tell us 2 important things:

+ ① Gradient of the graph = the acceleration

The equation for acceleration  $\Rightarrow$  
$$a = \frac{v-u}{t}$$

$$\therefore \text{for } ① \Rightarrow a = \frac{10\text{ms}^{-1} - 0\text{ms}^{-1}}{2} = 5\text{ms}^{-2}$$

where  $a$  = acceleration  
 $v$  = final velocity  
 $u$  = initial velocity  
 $t$  = time taken.

- The units of acceleration are  $\text{ms}^{-2}$  or  $\text{m/s}^2$  or  $\text{m/s/s}$ .

for ② the gradient = 0  $\therefore$  no acceleration  $\Rightarrow$  CONSTANT VELOCITY.

$$\text{for } ③ \quad a = \frac{v-u}{t} = \frac{0 - 10\text{ms}^{-1}}{2} = -5\text{ms}^{-2}$$

the negative gradient is called a DECELERATION

+ ② The second important fact is:

AREA UNDER A VELOCITY-TIME GRAPH = DISPLACEMENT

[Remember that  $D = S \times t$ ]  $\therefore$  it follows.

$$\begin{aligned} \text{From graph } \Rightarrow \text{area } a &= \text{triangle} \therefore \text{area} = \frac{1}{2} b \times h \\ &= \frac{1}{2} \times 2\text{s} \times 10\text{ms}^{-1} \end{aligned}$$

$$\text{DISPLACEMENT} = \underline{\underline{5\text{m}}}$$

- By summing areas ① + ② - ③ we can get the total displacement by the object.

## FORCES

- A force is effectively a Push or a Pull on an object.
- Force is a vector quantity
- IMPORTANT FORCES :

WEIGHT - due to the gravitational field strength.

TENSION - When an object is pulled at both ends. e.g. rope in tug of war

COMPRESSION - When an object pushed at both ends e.g. pillars in building

FRICITION - resistive force between two objects that opposes motion e.g. brick sliding over desk, brake pads against brakes in a car.

NORMAL REACTION - The contact force exerted by the surface that supports an object, and it acts perpendicular to the surface (hence Normal).

NEWTONS 3 LAWS - help us understand how forces affect mechanical situations.

NEWTONS 1<sup>ST</sup> LAW - Objects continue to move at constant velocity (which may be zero) until they acted upon by a resultant force.

Simplified this can be stated as: When no unbalanced forces acts on an object, its state of motion will be unchanged. Either a body remains at rest, or it carries on moving in a straight line at a constant velocity.

## NEWTONS 2<sup>ND</sup> LAW

Newton discovered that for a fixed mass :  $F_r \propto a$

and for a constant resultant force  $F_r$  :  $a \propto \frac{1}{m}$

This gives  $\Rightarrow$  Newton II<sup>nd</sup> Law

$$\underline{F_{\text{resultant}} = \text{mass} \times \text{acceleration}} \quad \text{or} \quad \overrightarrow{F} = ma$$

$\therefore$  A force of 1N accelerates a mass of 1kg at  $1\text{ ms}^{-2}$

• It is vital that the term 'resultant force' is understood:

The resultant force is the 'unbalanced force'!

Example



Space Shuttle:

Engine produced an upward thrust force  $F_T$

Spaceshuttle has Weight of  $W$ .

FACT:  $F_T$  must be greater than  $W$  for Spaceshuttle to lift off.

∴ What is the resultant force, and ∴ the acceleration

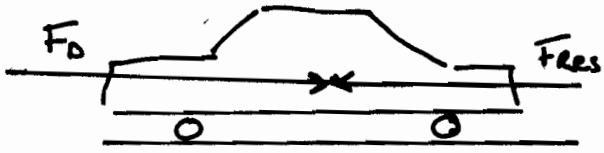
$$F_R = m \cdot a.$$

$$\text{but } F_R = F_T - W \quad \therefore (F_T - W) = ma$$

effectively, the resultant force = "the difference" or unbalanced force.

EXAMPLE

CAR is travelling on motorway.



$F_D$ : Force driving from engine

$F_{res}$ : Drag forces from air resistance etc.

Three possible scenarios:

① Car accelerates ∴  $F_D > F_{res} \quad \therefore F_D - F_{res} = F_R = ma$   
∴  $a = +ve$  acceleration.

② Car at Constant Velocity ∴  $F_D = F_{res} \quad \therefore F_R = 0 \quad \therefore a = 0$

③ Car decelerates ∴  $F_D < F_{res} \quad \therefore F_D - F_{res} = -F_R = ma$   
∴  $a = -ve$  acceleration  
≈ DECELERATION.

## Understanding Terminal Velocity

- Terminal Velocity is reached due to the changing Resultant Force on an object. Let us look at the sequence of events:

- ① A ball is released from a given height:  $t_{\text{ini}} = 0 \quad (t=0)$

$$\text{Mass} = M,$$



- Ball has a Weight  $w$  due to mass  $M$ , and the gravitational field.
- Initially the resistive forces on the ball are zero as it has not started to collide with air molecules that will resist its path.

$$\therefore F_e = Ma$$

$$F_e = N \quad \therefore \quad W = Ma \quad \Rightarrow \quad M \cdot g = M \cdot a \\ a = g.$$

- ② As  $t$  increase, the object starts to build up opposing resistive forces.



$F_{\text{res}}$  increases as the object accelerates  
N remains, of course, constant

However  $W > F_{\text{res}}$

$$\therefore F_e = Ma$$

$W - F_{\text{res}} = Ma \quad \therefore a \downarrow$ , but the object still accelerates.

③  $t \uparrow$  further - we get to the stage where the relative forces are equal to the weight.



$$F_{\text{rel}} = W \quad \therefore F_e = W - F_{\text{rel}} = 0$$

$$\therefore a = 0$$

If  $a = 0$ , the object is at constant speed . or TERMINAL VELOCITY

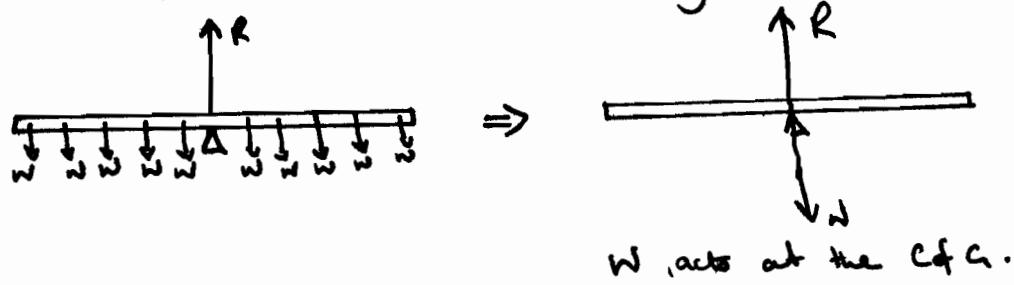
### CENTRE OF MASS + CENTRE OF GRAVITY

Centre of Mass of a body - is the point through which any applied force produces translation but no rotation.

Whereas,

Centre of Gravity - is the point at which the resultant force of gravity acts  $\Rightarrow$  the place where a single force equal to the weight of the object can replace the billions upon billions of individual gravitational forces acting on each particle that makes up the object.

In all GCSE problems it is normal for the CoM and the CofG to be in the same place, however, they are not the same thing.



$W$  acts at the CofG.

## TURNING EFFECTS - MOMENTS

- The turning effect of a force  $F$  about some axis is called its MOMENT.
- This can be thought of as the 'leverage' of a force, and is increased if the force is made larger or if its line of action is farther from the point considered.
- If the force acts in a plane perpendicular to the rotation axis, the moment is defined by:

Moment = magnitude of force  $\times$  perpendicular distance of the line of action of the force from the axis of rotation.

Unit = Nm.

A diagram of a wrench being used to turn a nut. A vertical force vector labeled  $F = 10\text{N}$  is shown acting downwards at the end of the wrench handle. The handle is horizontal and has a total length of  $0.5\text{m}$ , indicated by a double-headed arrow below it. The wrench is shown from a side-on perspective.

$$\begin{aligned}\therefore \text{Moment} &= F \times d \\ &= 10 \times 0.5 \\ &= \underline{5\text{Nm}}\end{aligned}$$

- Moments can be used to analyse several different systems.

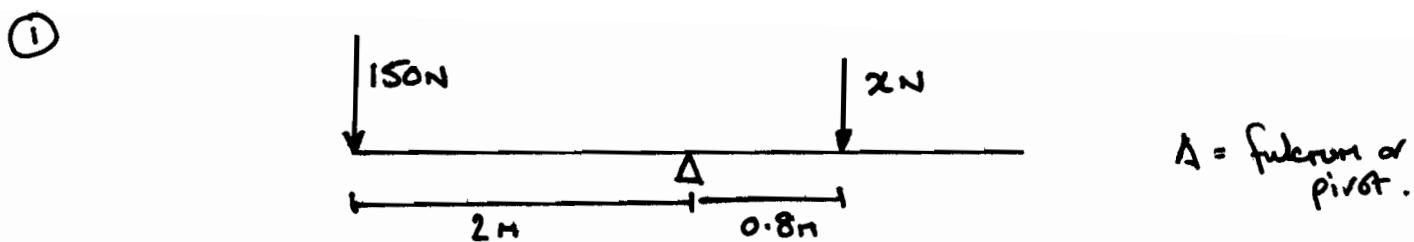
For a system to be in EQUILIBRIUM i.e. force are balanced,  
then :

The sum of the clockwise moments = sum of anticlockwise moments

$$\sum C \text{ moments} = \sum G \text{ moments.}$$

- We will analyse 2 basic system

- ① A see-saw.
- ② A bridge structure.



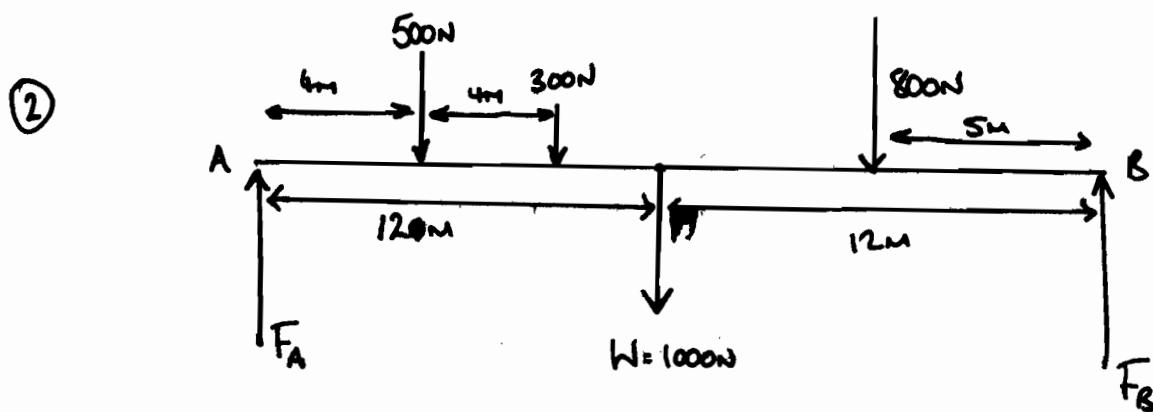
Determine the weight of  $x$ .

For equilibrium :  $\sum \text{clockwise moments} = \sum \text{anticlockwise moments}$

$$0.8m \times x = 2m \times 150N$$

$$0.8x = 300$$

$$\underline{x = 375N}$$



Force  $F_A$  and  $F_B$  are the supports of the bridge

$$\therefore F_A + F_B = 500N + 300N + 1000N + 800N \quad (\text{Forces up = forces down})$$

$$F_A + F_B = 2600N \quad (\text{must be for equilibrium.})$$

- Taking moments about point A:

$$\sum \text{clockwise moments} = \sum \text{anticlockwise moments}$$

$$\therefore (500N \times 4m) + (300N \times 8m) + (1000N \times 12) + (800N \times 19m) = F_B \times 24m$$

$$31600N \cdot m = F_B \times 24m$$

$$\underline{F_B = 1317N}$$

Using  $F_A + F_B = 2600N \Rightarrow F_A = \underline{1283N}$

By varying the weights  $F_A$  &  $F_B$  will vary in magnitude.

## Hooke's Law

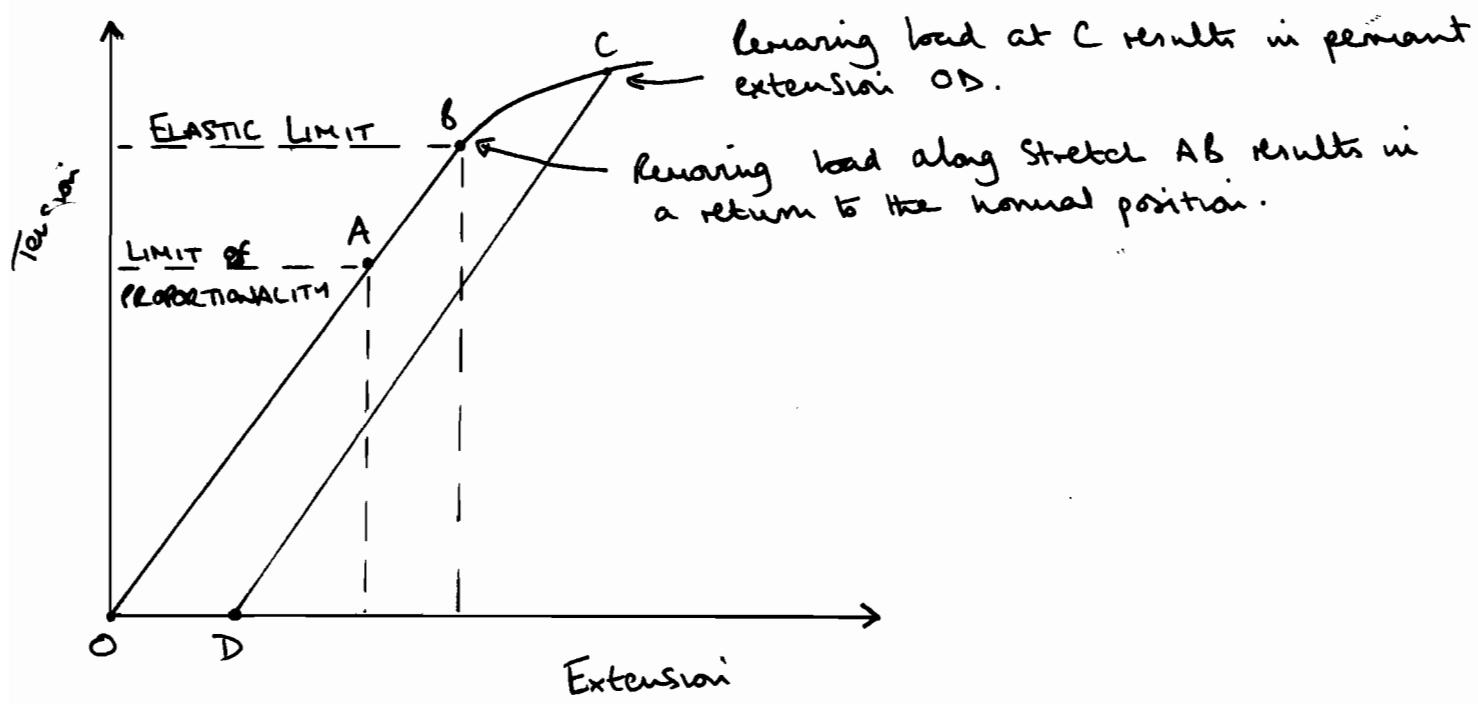
- For many objects the force  $F$  required to maintain an extension,  $x$ , is directly proportional to the extension.

$$F \propto x \quad \text{which gives} \quad F = kx$$

Where  $k$  is the Spring constant and is a measure of the 'Stiffness' in  $\text{N m}^{-1}$

Hooke's Law is usually obeyed up to some maximum value of the applied force, and beyond that the relation between force and extension is non-linear.

### STRETCHING A HELICAL STEEL SPRING:



Spring Constant:  $k = \frac{F}{x}$  equal gradient of graph in the linear region.

Limit of Proportionality: beyond this point (A) the graph is non-linear.

Elastic behaviour: means that the ~~the~~ spring returns to zero

extension when the load is removed.

Elastic Limit: beyond this point (b) the spring suffers permanent deformation, and does not return to zero extension when the load is removed.

Plastic Deformation: permanent structural change, after which the spring will not return to zero extension when the load is removed.

In the elastic region, the applied forces extend the bonds between particles in the material. Permanent or plastic deformation occurs when bonds break and particles move & or flow past one another to new positions.

## SPRINGS IN SERIES + PARALLEL.

### SERIES



We know that for Hooke's law

$$F = k e$$

$F$  = force,  $k$  = spring constant,  $e$  = extension

Having in series effectively reduces the stiffness of the system:

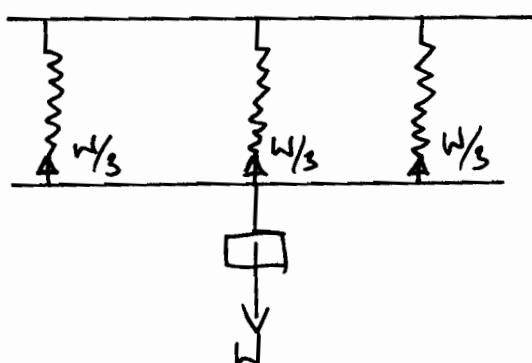
$$\text{Series} \Rightarrow \frac{k}{n}$$

$$\therefore F = \frac{k}{n} \cdot e$$

The arrangement is less stiff than a single spring.

$$\therefore e = \frac{Fn}{k} \quad \therefore e \uparrow \text{factor } n$$

### PARALLEL



From Hooke's Law:

$$F = k e$$

For parallel  $\Rightarrow n k$

$$\therefore F = n k e$$

$$\therefore e = \frac{F}{n k} \quad \therefore e \downarrow \text{by factor } \frac{1}{n}.$$

This system is stiffer than a single spring

## Springs in series and parallel

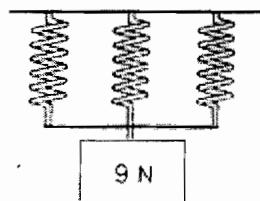


Fig. 1.1

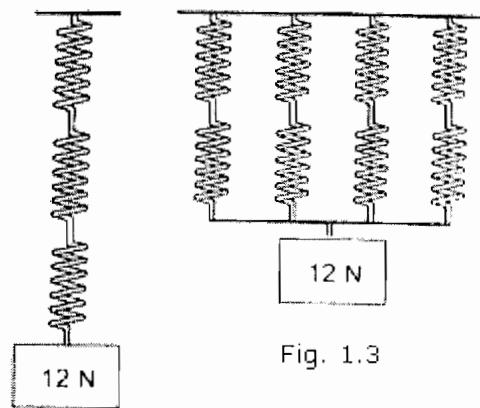


Fig. 1.2

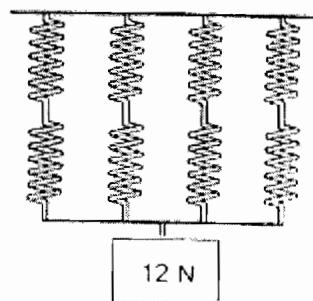


Fig. 1.3

Identical springs are used in the arrangements shown above. The diagrams are not shown to scale, and the unstretched lengths of the springs are in fact different in the four diagrams. In Fig. 1.1, the 9 N weight hangs 1.5 cm below the unstretched position of the springs.

- (a) Calculate the total extensions of the arrangements in Fig. 1.2 and 1.3 for the loads shown.

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[4]