

# JP Waves Demonstration Circus



OSCILLOSCOPE OS-5020 20MHz

Dr Andrew French. Winchester College. January 2018.

# **JP Waves Circus Demonstrations**

1. Slinkies
2. Tuning forks, a microphone and an oscilloscope
3. Measuring the speed of sound
4. Measuring the speed of light in a conductive cable
5. Kundt's tube
6. Rubens' tube
7. Signal generator, oscilloscope & spectrogram via MATLAB SoundAnalyser
8. Signal generator and two-speaker sound interference recorded using a CRO + microphone
9. Diffraction of water waves using a ripple tank



# JP Waves Circus Demonstrations

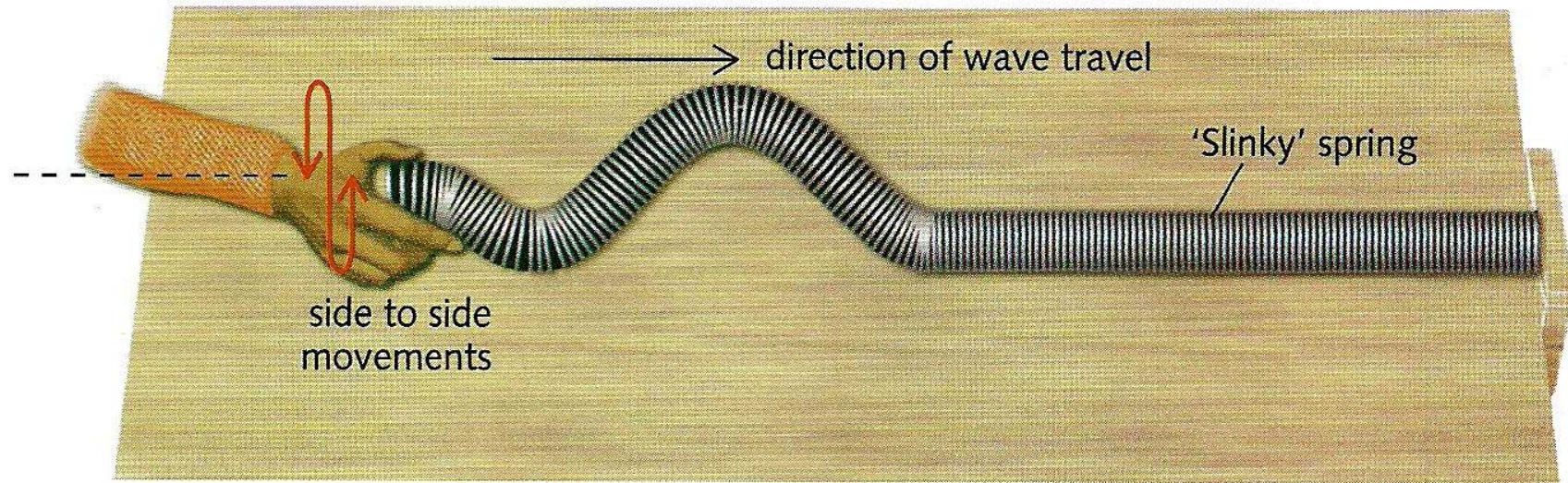
## # Slinkies

- Idea of wave being a *disturbance*
- Longitudinal vs transverse waves
- Speed of waves varies with slinky tension
- $180^\circ$  phase change on reflection from fixed end
- Idea of standing waves – *nodes* and *antinodes*

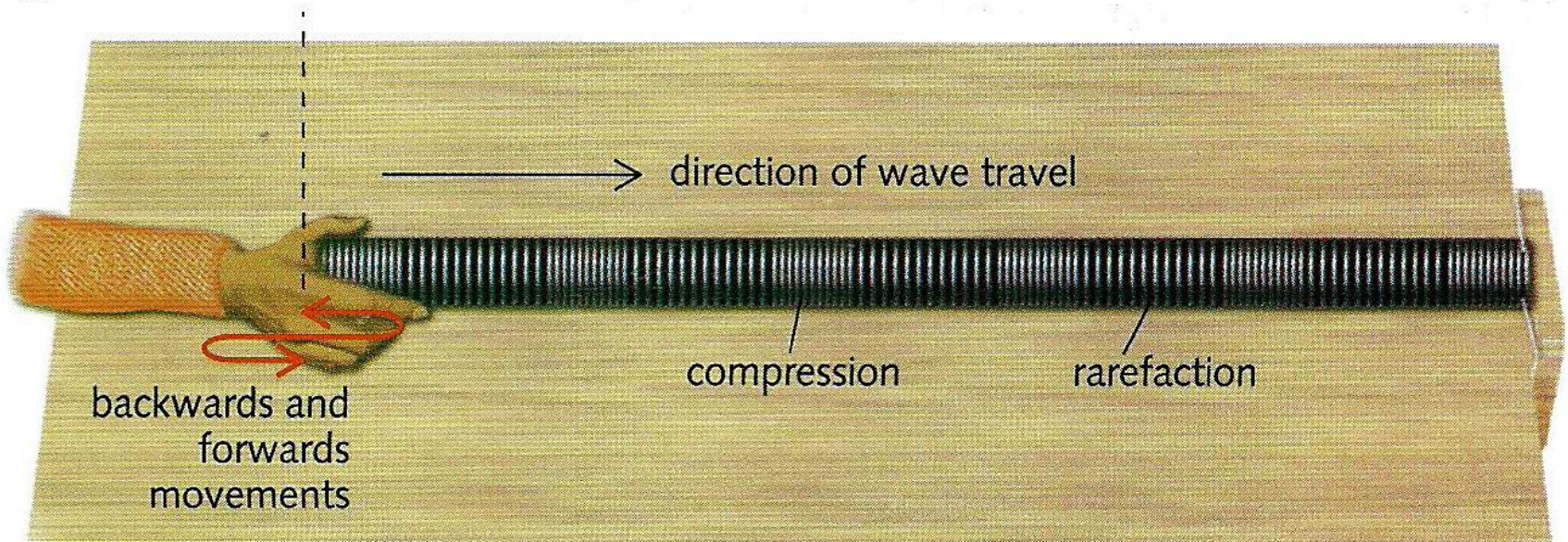




# Transverse waves



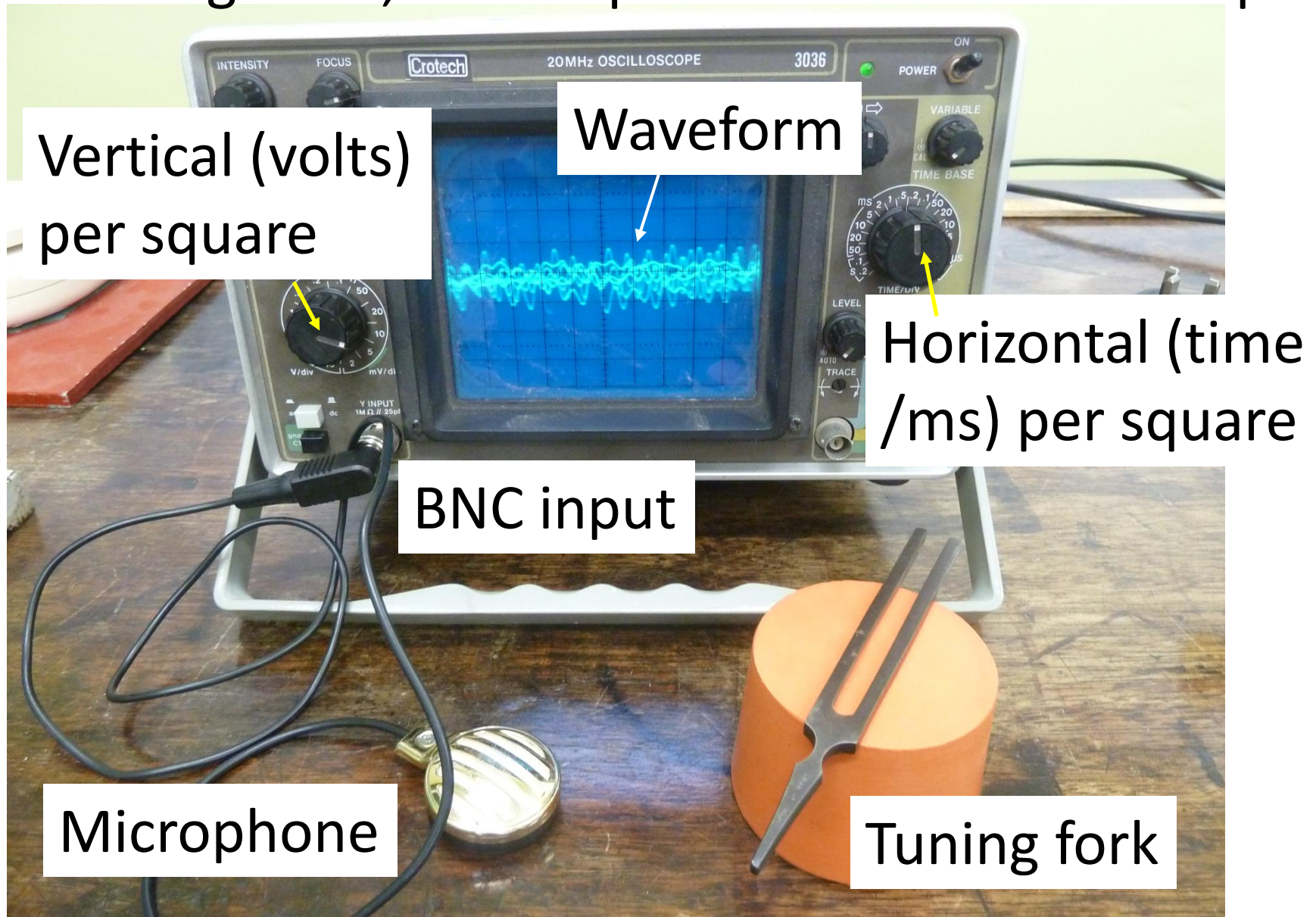
# Longitudinal waves





# JP Waves Circus Demonstrations

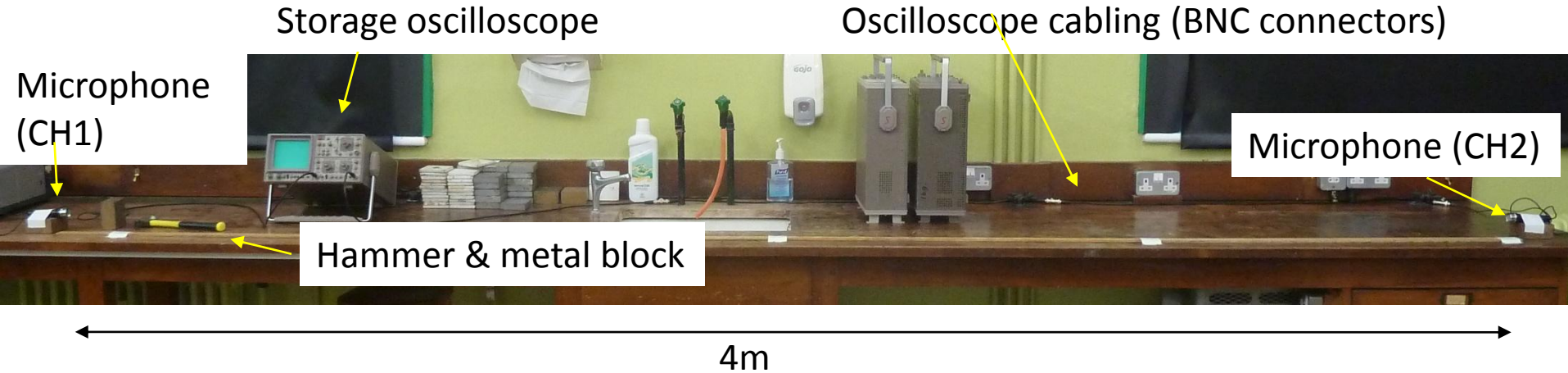
## #2 Tuning forks, a microphone and an oscilloscope





# JP Waves Circus Demonstrations

## #3 Measuring the speed of sound

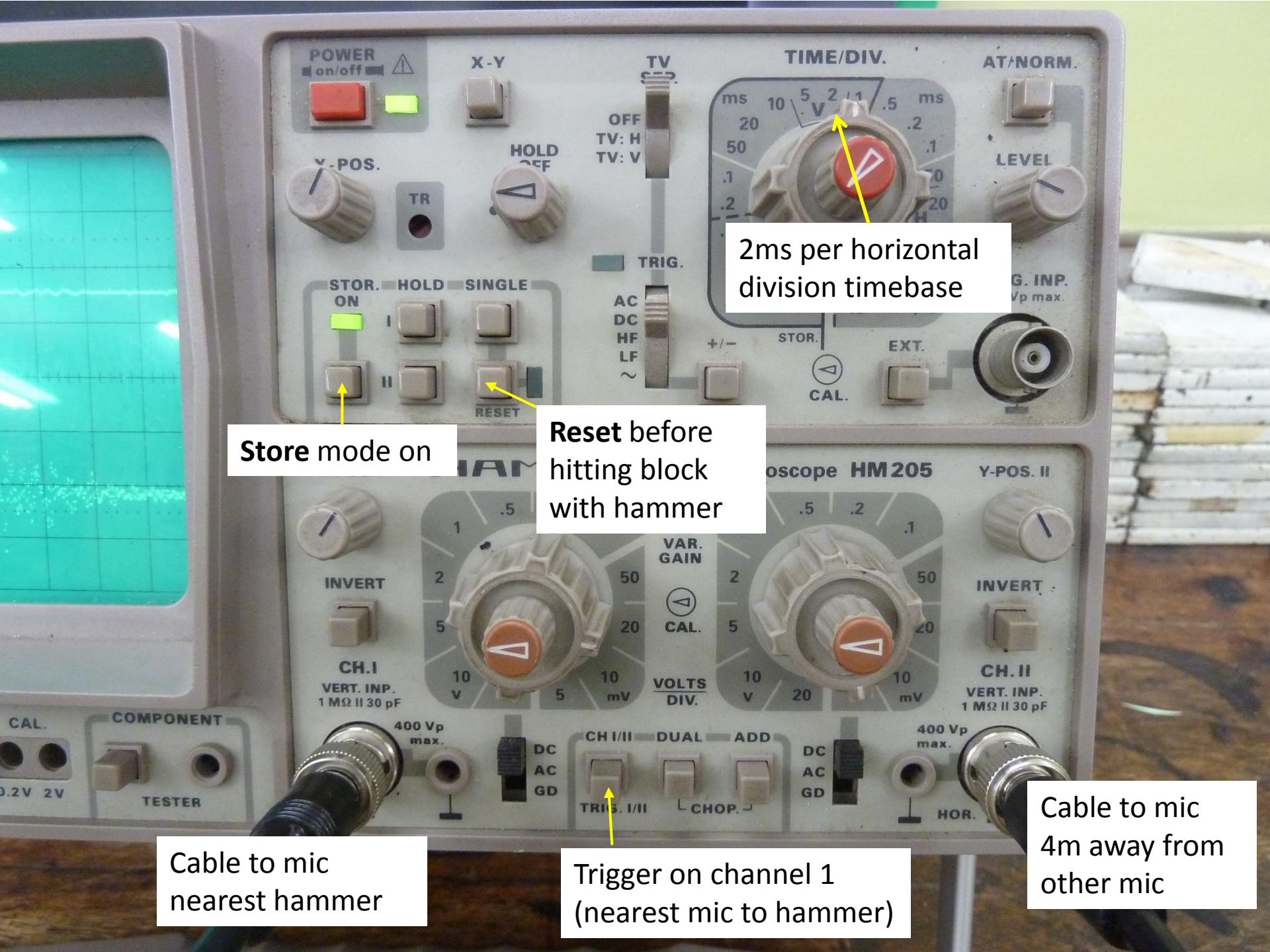


Pick up block and strike with hammer to produce a sound pulse. Pick up block to avoid bench vibration.

Strike *behind* mic so CRO triggers when sound wave reaches this mic. The recorded delay is therefore the separation between the microphones.







2ms per horizontal division timebase

Store mode on

Reset before hitting block with hammer

Cable to mic nearest hammer

Trigger on channel 1 (nearest mic to hammer)

Cable to mic 4m away from other mic



**Channel 1**

Triggers when sound pulse reaches it

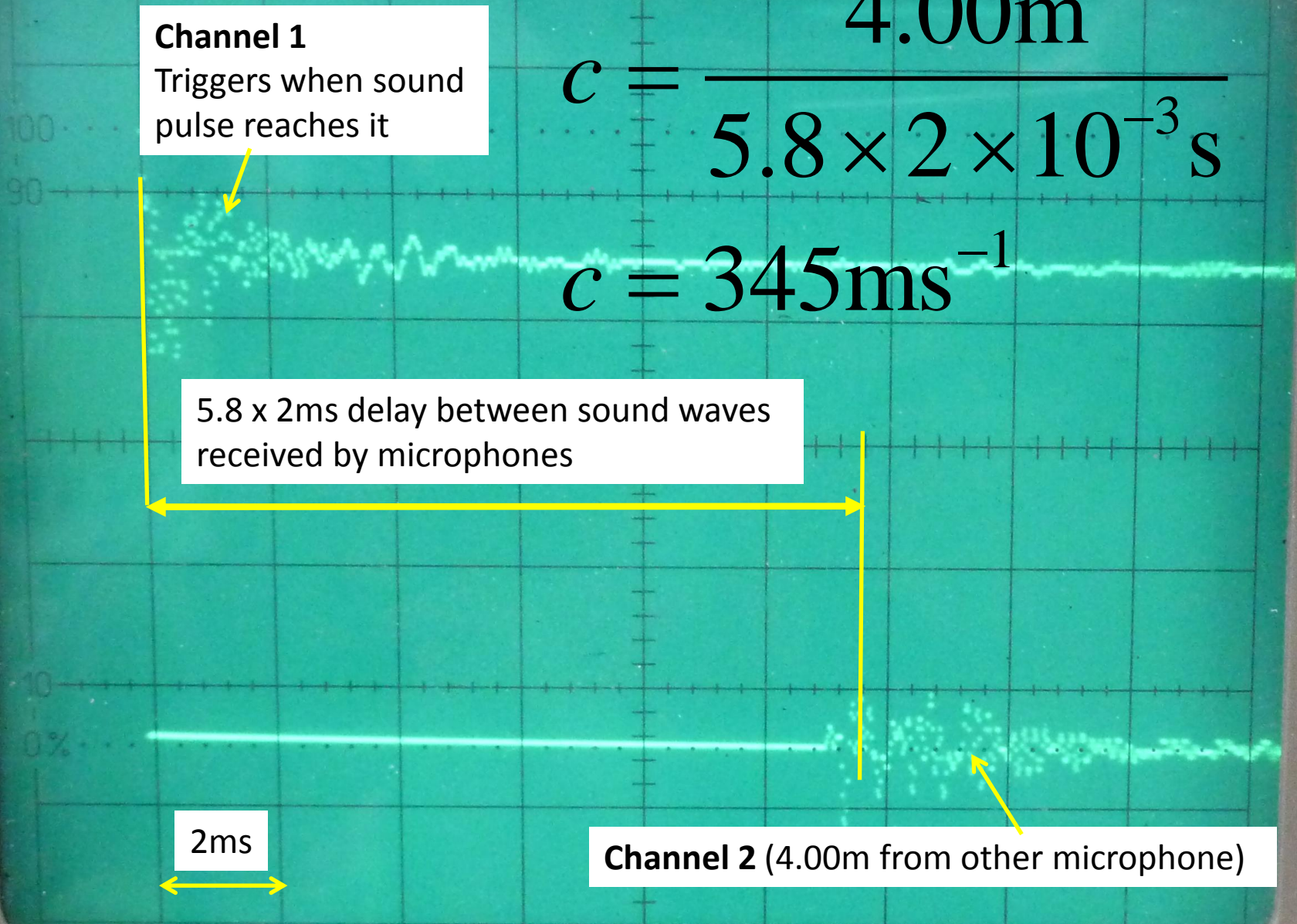
$$c = \frac{4.00\text{m}}{5.8 \times 2 \times 10^{-3}\text{s}}$$

$$c = 345\text{ms}^{-1}$$

5.8 x 2ms delay between sound waves received by microphones

2ms

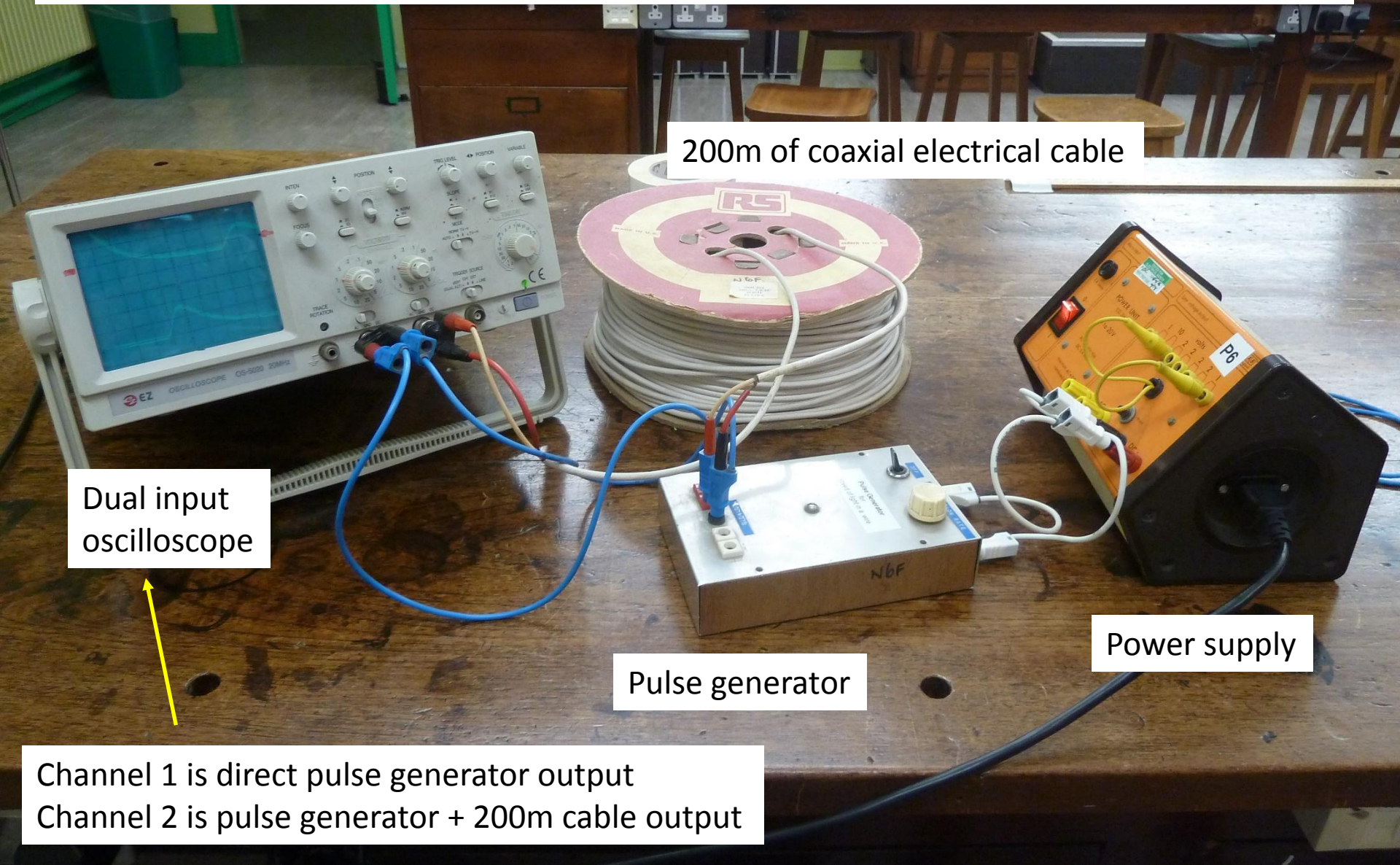
**Channel 2** (4.00m from other microphone)





# JP Waves Circus Demonstrations

## #4 Measuring the speed of light in a coaxial cable



200m of coaxial electrical cable

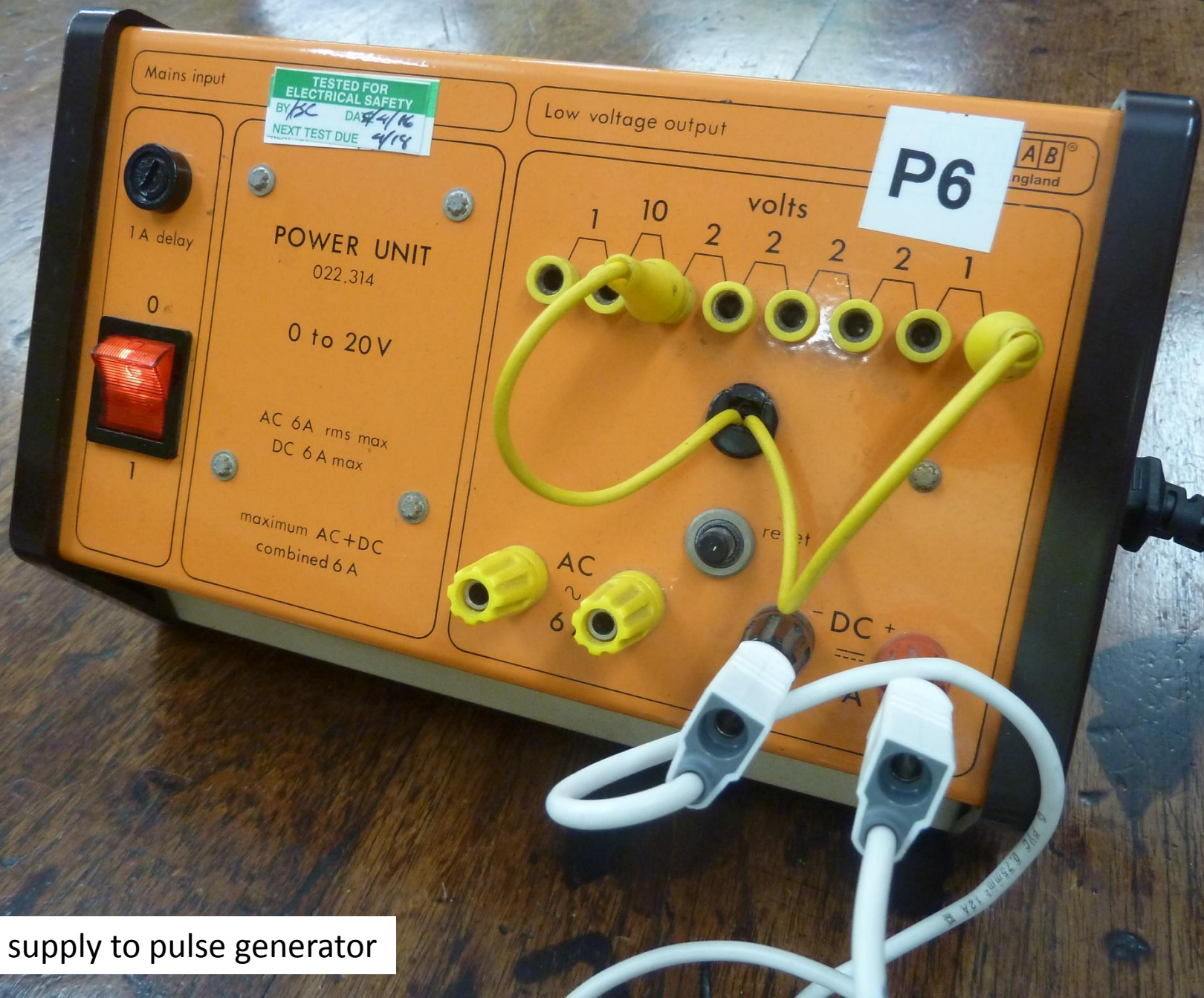
Dual input  
oscilloscope

Pulse generator

Power supply

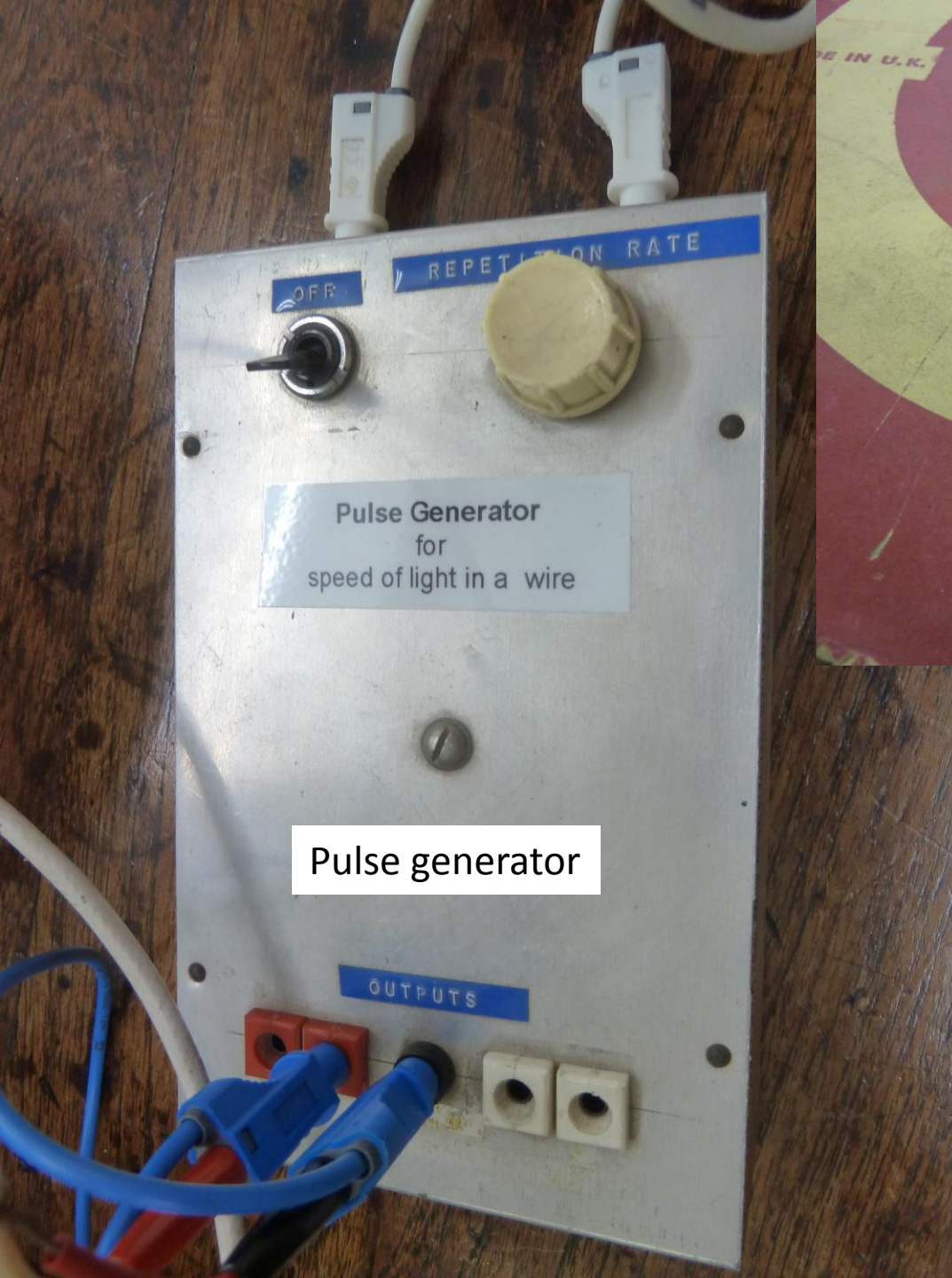
Channel 1 is direct pulse generator output  
Channel 2 is pulse generator + 200m cable output





9V DC supply to pulse generator





Pulse generator



Wire specification



Increase timebase to see pulses, and reflections. The reflections are off the end of the 200m cable i.e. they correspond to a 'there-and-back' round trip of 400m.

Pulse 1

Pulse 2

Pulse 3

Reflections

**Channel 1**

(direct output of pulse generator)

5  $\mu$ s timebase

**Channel 2**

(direct output pulse generator  
+ 200m cable)

Here there will be a *phase shift*  
corresponding to the delay resulting  
from the extra 200m of propagation

Set oscilloscope trigger on channel 1



Although the time delay between channels can be used to calculate the propagation speed, uncertainty when triggering *actually* occurs means the *reflections* are perhaps a less error prone source of measurement.

$$c = \frac{800\text{m}}{6.8 \times 0.5 \times 10^{-6}\text{s}}$$
$$c = 2.35 \times 10^8 \text{ms}^{-1}$$

78% of the speed of light in a vacuum  
i.e. a **refractive index** of about 1.27

6.8 x 0.5μs

Each reflection corresponds to 2 x 200m = 400m.  
So the time delay above corresponds to 800m.

0.5 μs timebase



## COAXIAL CABLE



Electromagnetic waves travel at speed  $v$  in the coaxial cable

$$v = \frac{c}{\sqrt{\epsilon}}$$

Speed of light in vacuum  
 $2.998 \times 10^8 \text{ ms}^{-1}$

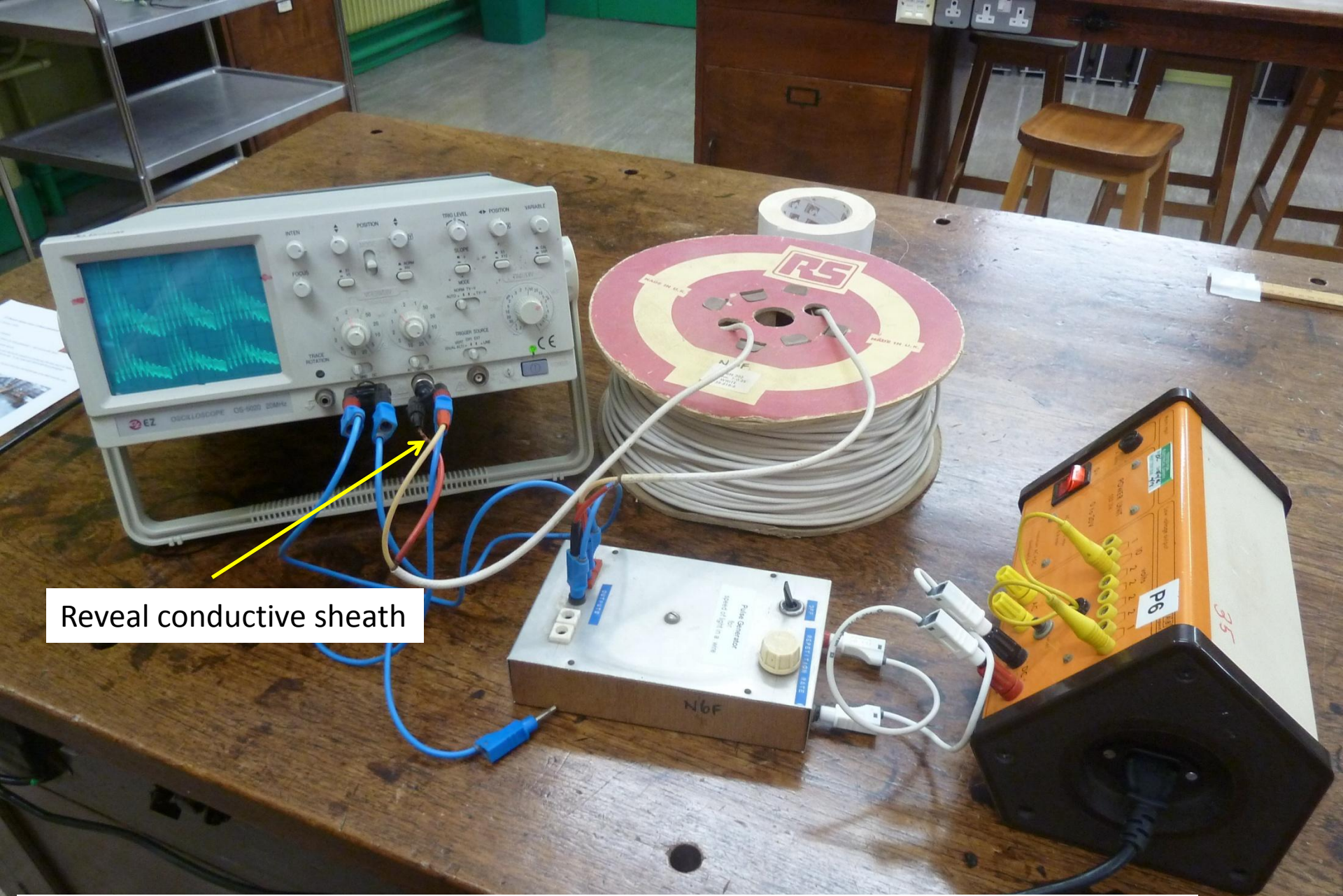
Relative Permittivity of dielectric

So the relative permittivity of our dielectric is predicted to be:

$$\epsilon = \left( \frac{c}{v} \right)^2 = 1.27^2 = 1.62$$

Note [relative permittivity of PTFE](#) is about 2.1





Reveal conductive sheath

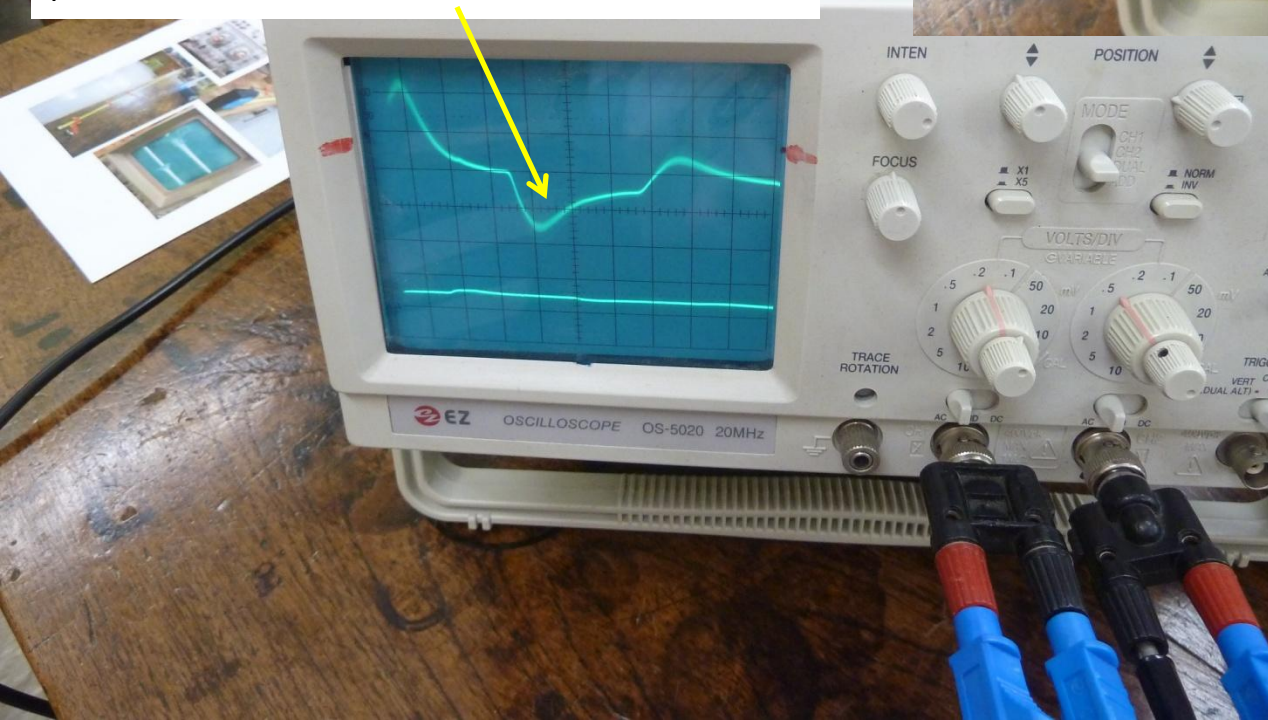
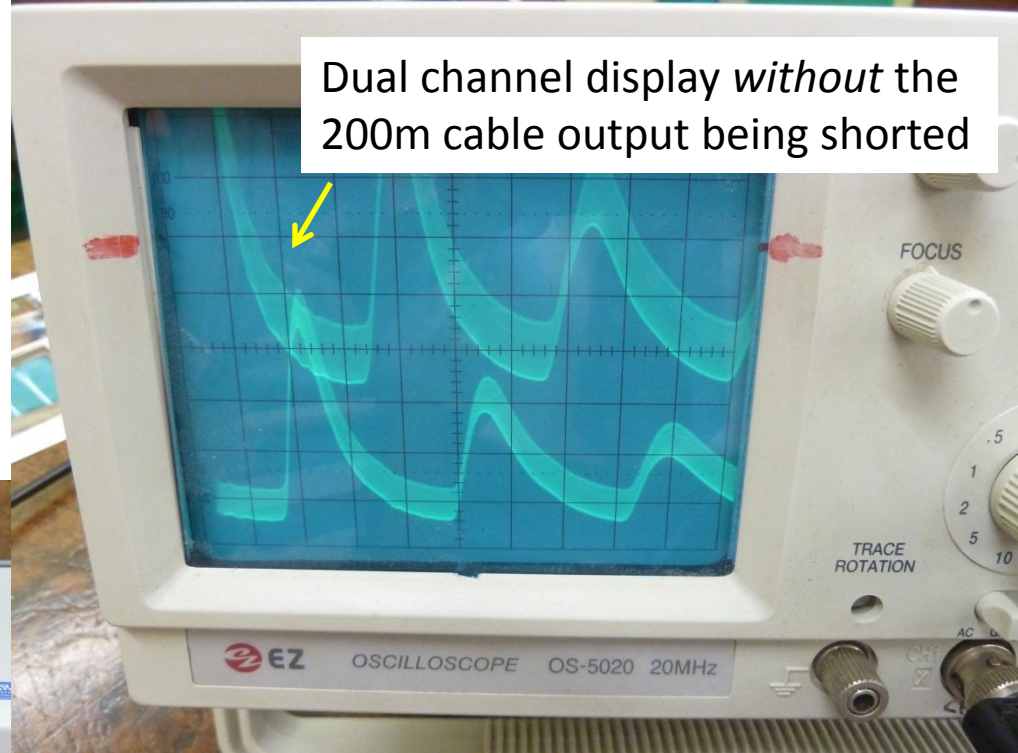
Add extension wire and 'reveal conductive sheath' to enable the 200m cable output to be optionally shorted



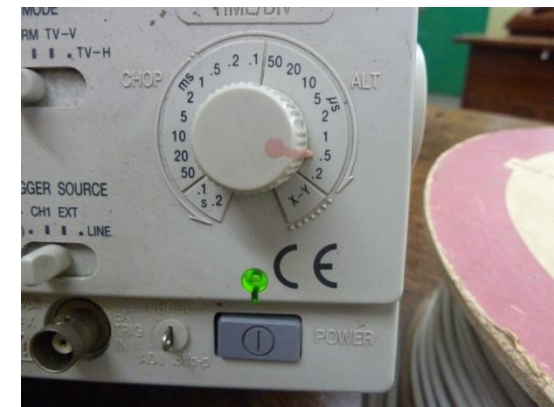
After 200m cable has been shorted.  
Note this causes the second reflection to be *inverted*.

Unlike the unshorted case, the reflected pulses are phase shifted by  $180^\circ$  when they reflect of the end of the cable.

This also explains why only odd numbered pulses are inverted.



0.5  $\mu$ s timebase



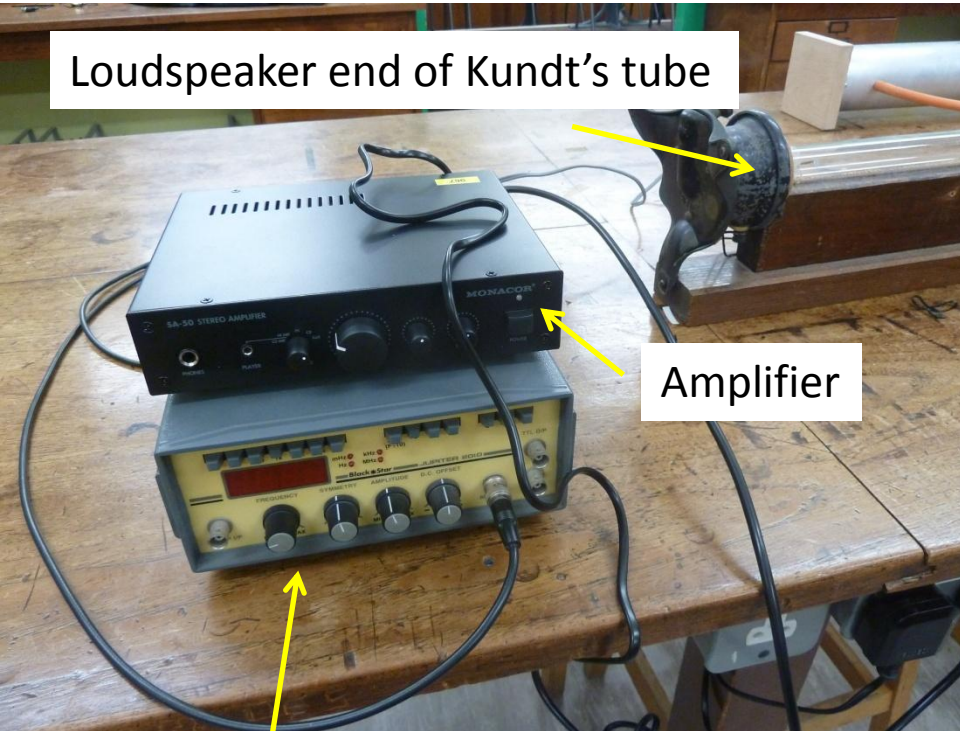


# JP Waves Circus Demonstrations

## #5 Kundt's tube



August Kundt  
1839-1894

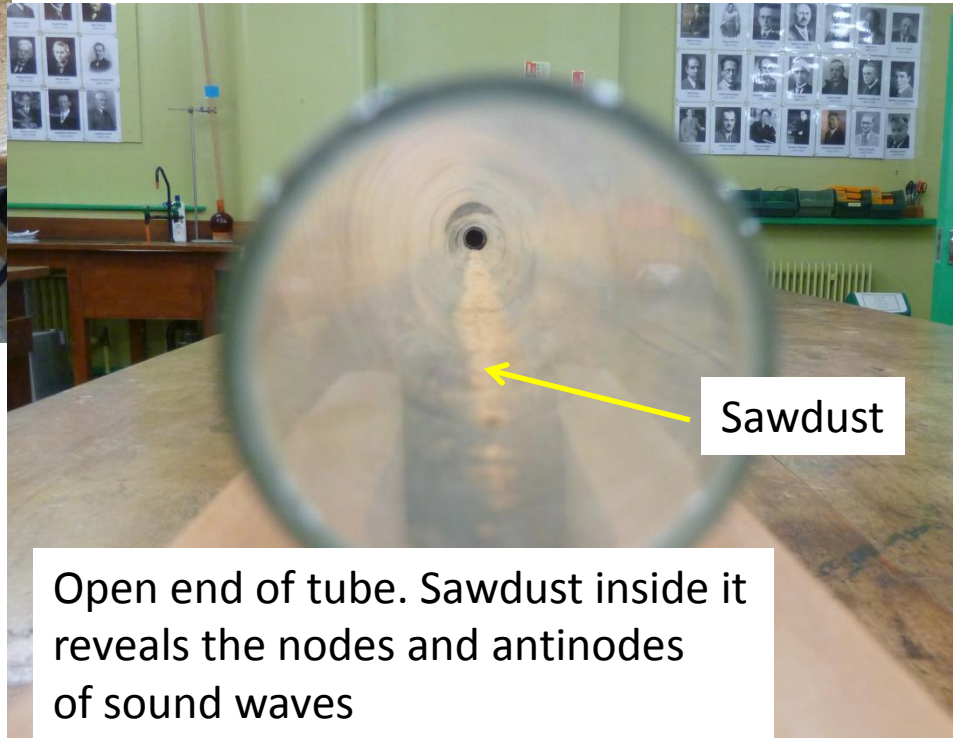


Loudspeaker end of Kundt's tube

Amplifier

Signal generator

**\* Wear ear defenders! \***



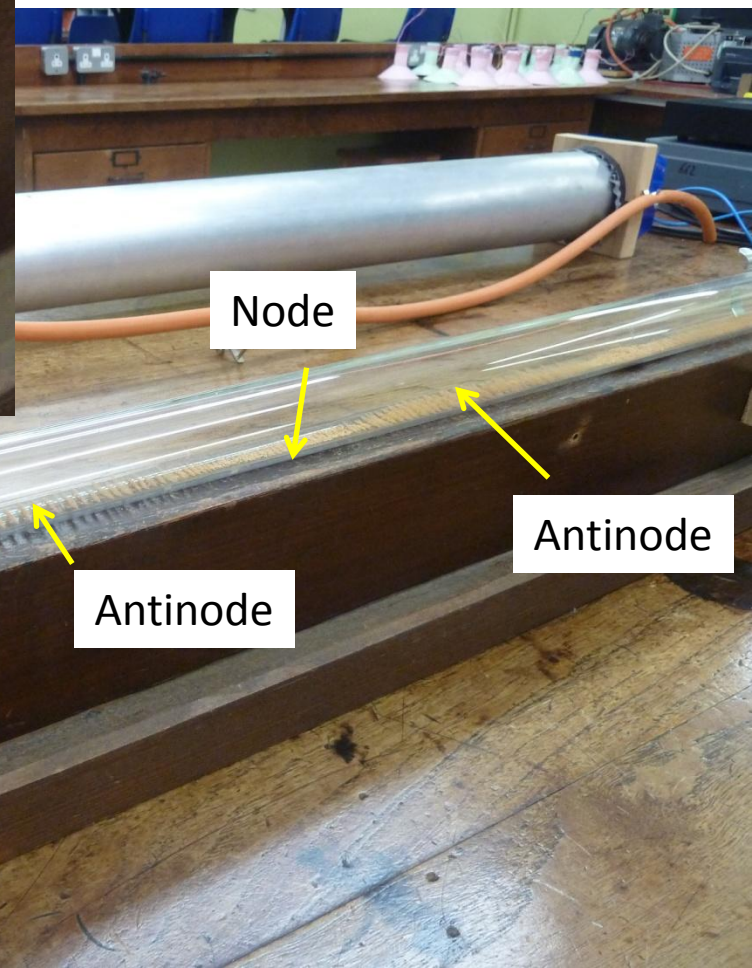
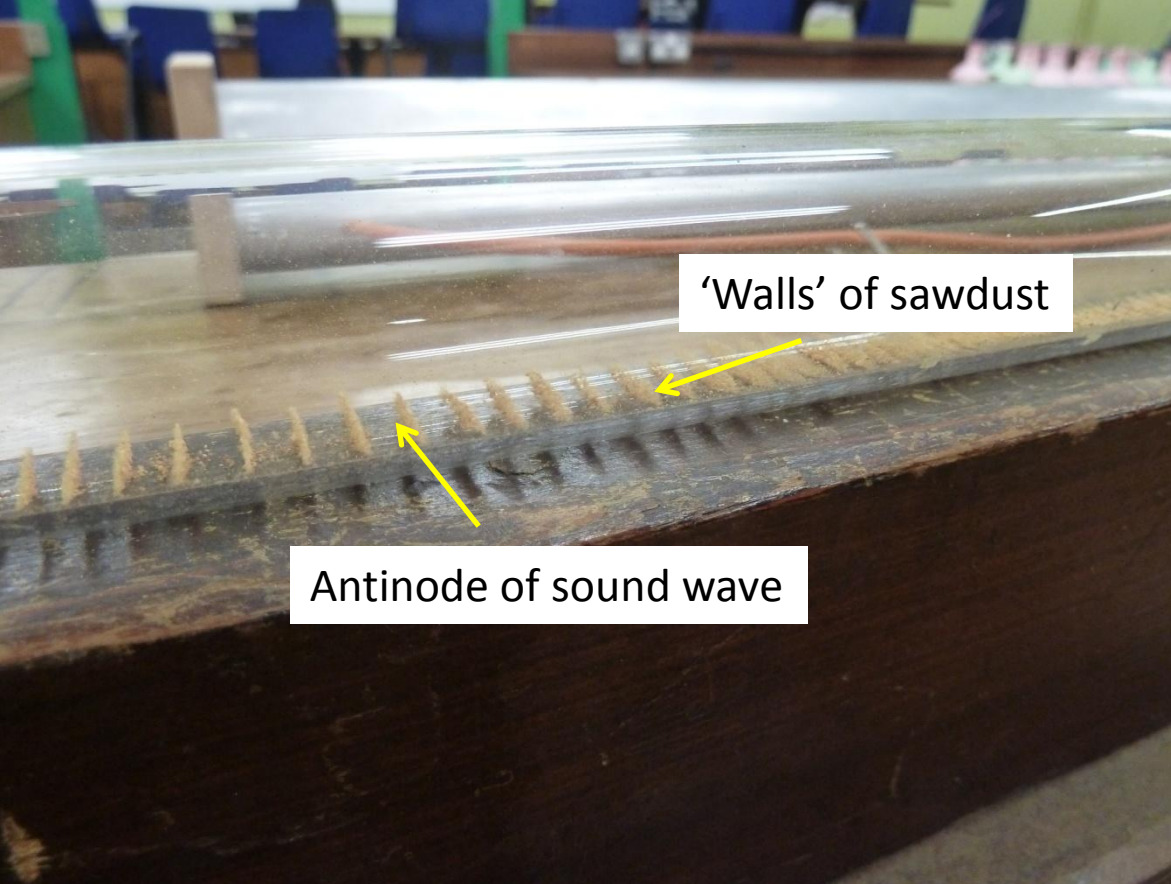
Sawdust

Open end of tube. Sawdust inside it reveals the nodes and antinodes of sound waves







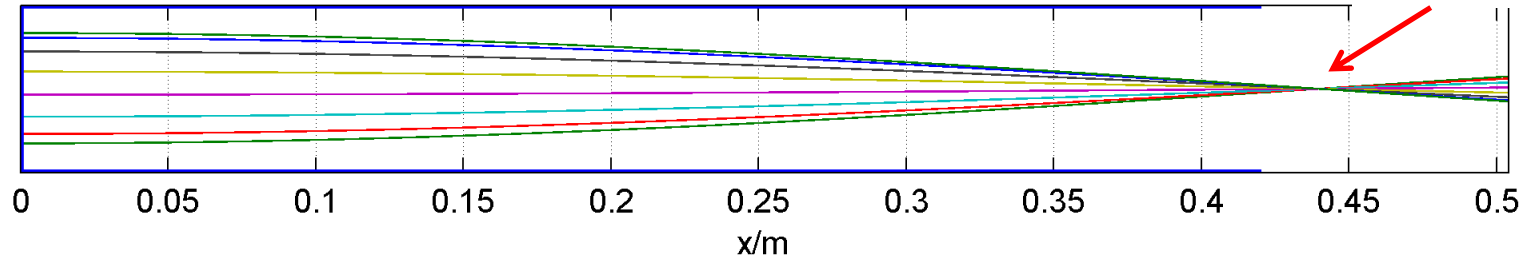


Note *air pressure antinodes*  
are *air displacement nodes*  
and vice versa



PRESSURE:  $L = 0.42\text{m}$ , Fundamental frequency =  $193.2697\text{Hz}$ ,  $\lambda = 1.7592\text{m}$

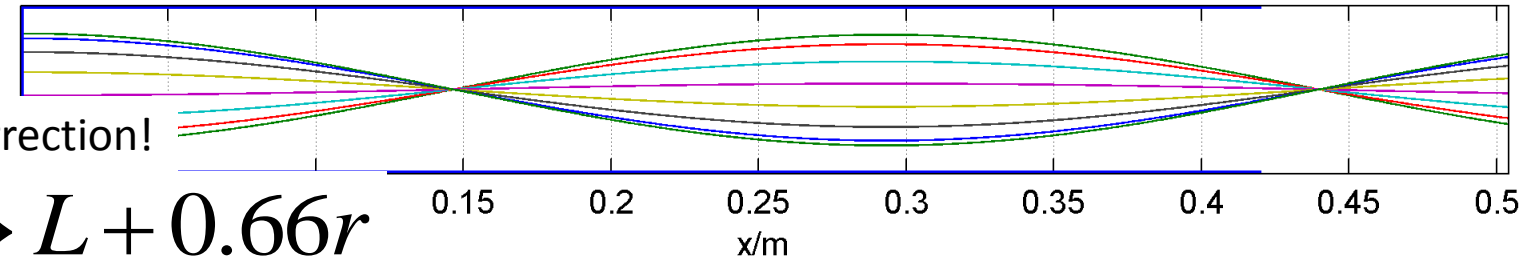
Pressure nodes



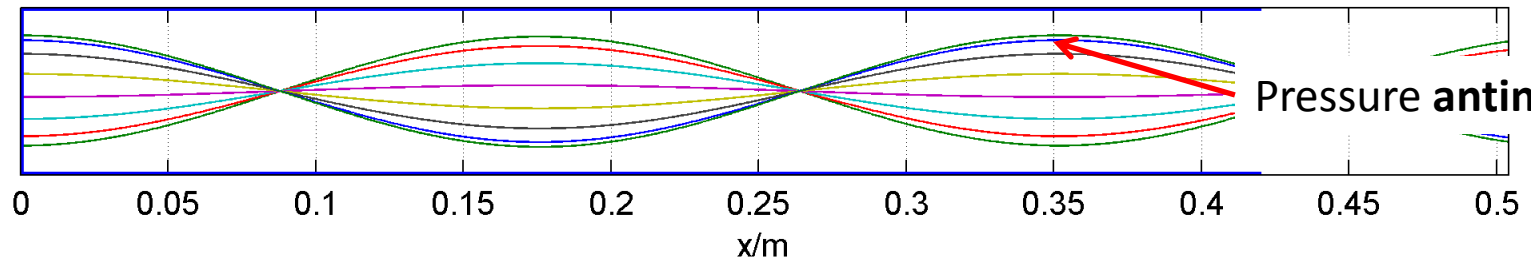
Harmonic #1 frequency =  $579.809\text{Hz}$ ,  $\lambda = 0.5864\text{m}$

End correction!

$$L \rightarrow L + 0.66r$$

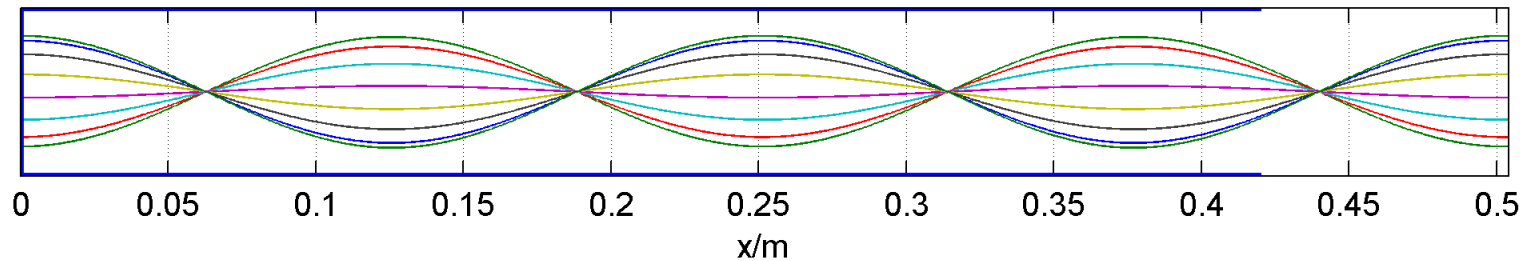


Harmonic #2 frequency =  $966.3483\text{Hz}$ ,  $\lambda = 0.35184\text{m}$



Pressure antinodes

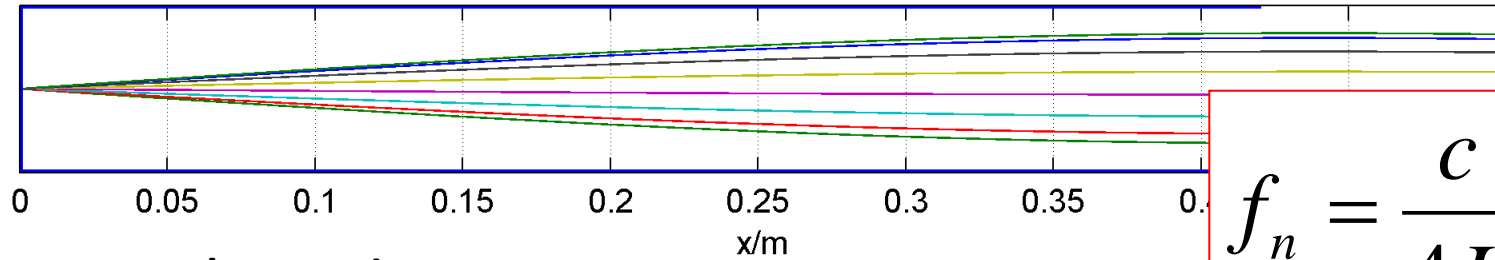
Harmonic #3 frequency =  $1352.8877\text{Hz}$ ,  $\lambda = 0.25131\text{m}$



Standing waves in an **open ended tube**: Air pressure vs distance at times within a wave period

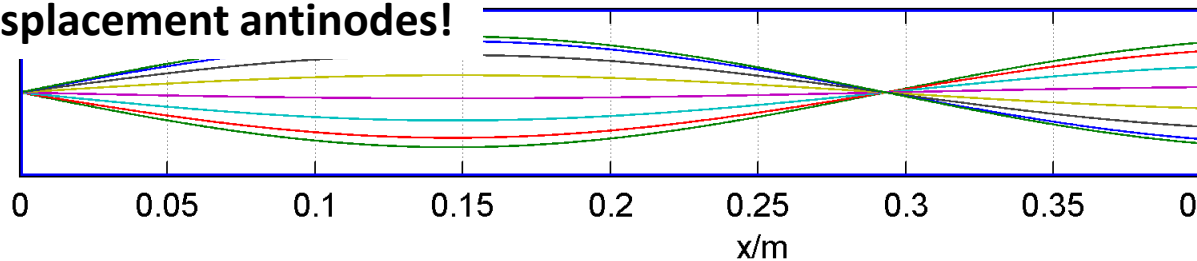


DISPLACEMENT:  $L = 0.42\text{m}$ , Fundamental frequency =  $193.2697\text{Hz}$ ,  $\lambda = 1.7592\text{m}$

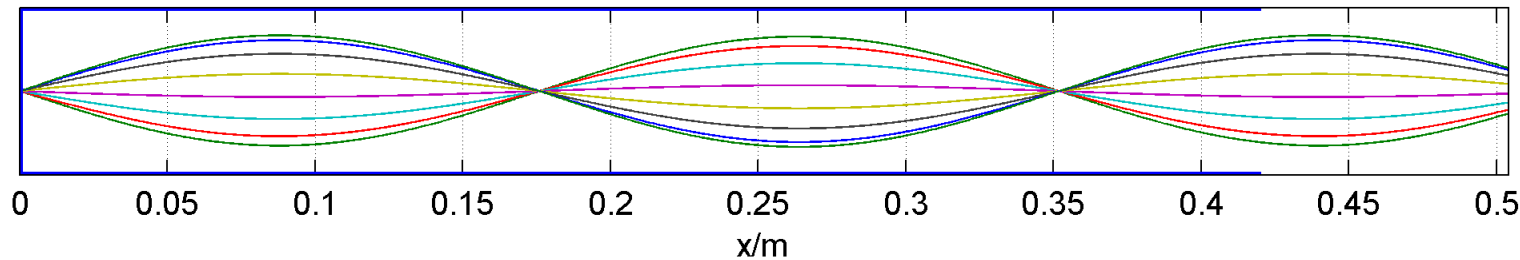


Pressure **nodes** are air  
**displacement antinodes!**

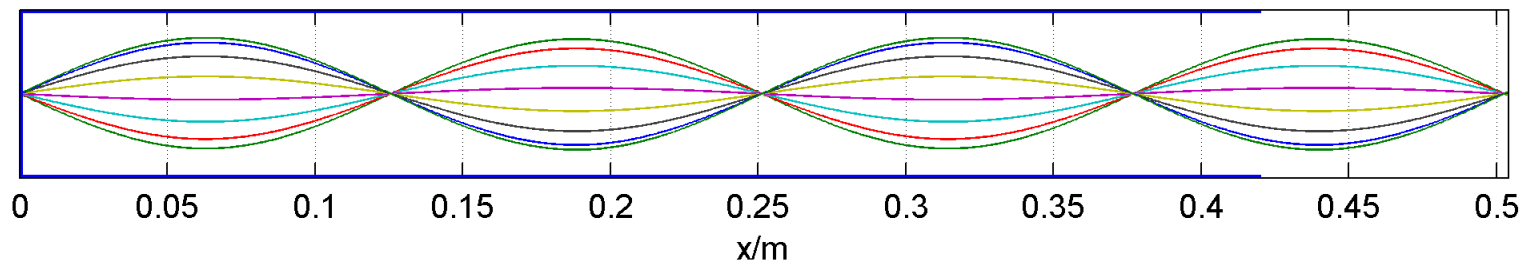
Harmonic #1 frequency =  $579.809\text{Hz}$ ,  $\lambda = 0.5864\text{m}$



Harmonic #2 frequency =  $966.3483\text{Hz}$ ,  $\lambda = 0.35184\text{m}$



Harmonic #3 frequency =  $1352.8877\text{Hz}$ ,  $\lambda = 0.25131\text{m}$



$$f_n = \frac{c}{4L}(2n-1)$$

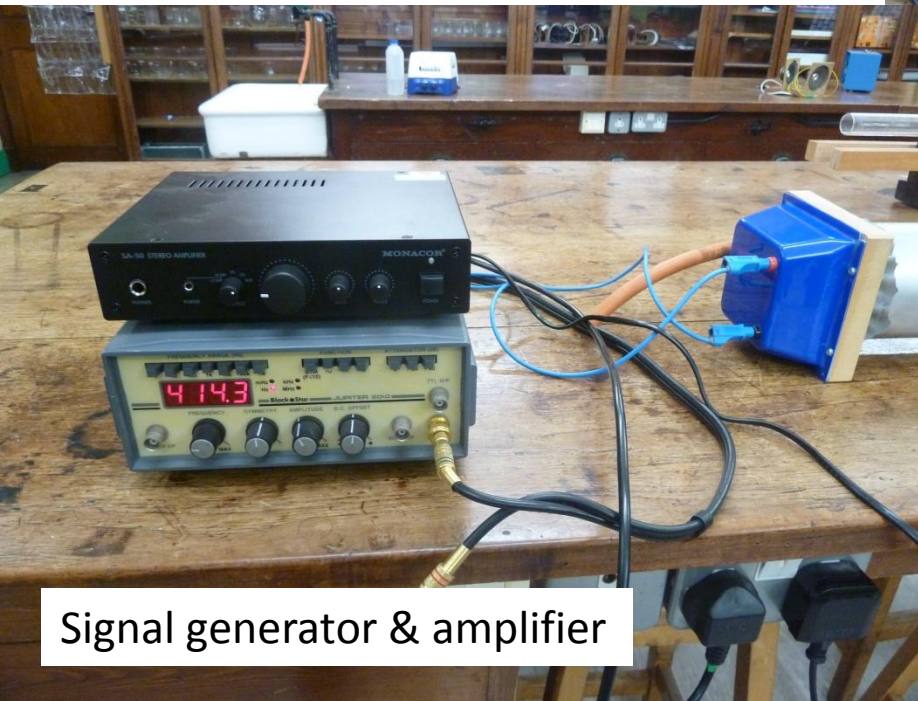
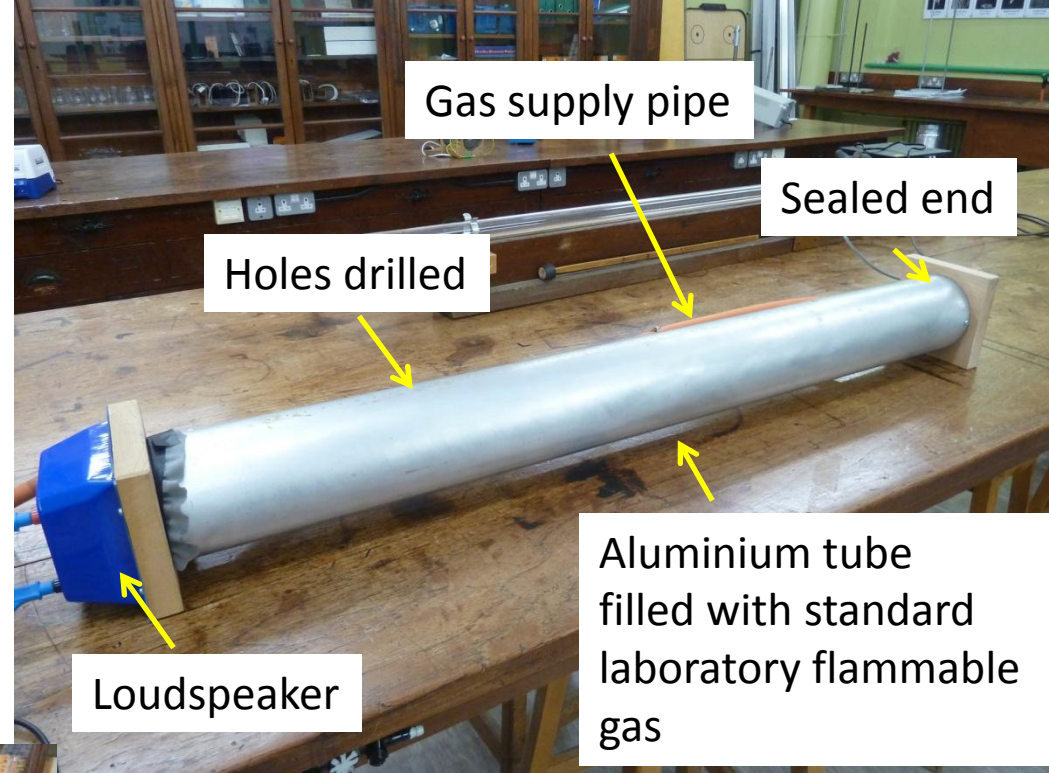
$$\lambda_n = \frac{c}{f_n} = \frac{4L}{2n-1}$$

Standing waves in an **closed ended tube**: Air displacement vs distance vs  $t$  within a wave period



# JP Waves Circus Demonstrations #6 Rubens' tube

Heinrich Rubens  
1865-1922



Allow gas to enter tube and then light the holes with a match or lit splint. Move along tube to align the fifty or so holes.

As a sound wave is set up in the tube, the pattern of pressure nodes and antinodes will result in different heights of flames.





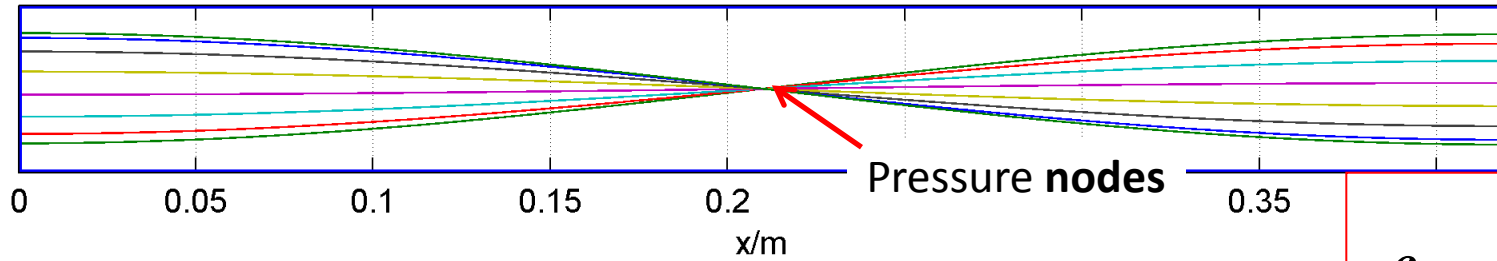
## The Boy Who Played with Fire!

Get enhanced flame height when gas pressure differs the most from atmospheric pressure i.e. at **pressure antinodes**

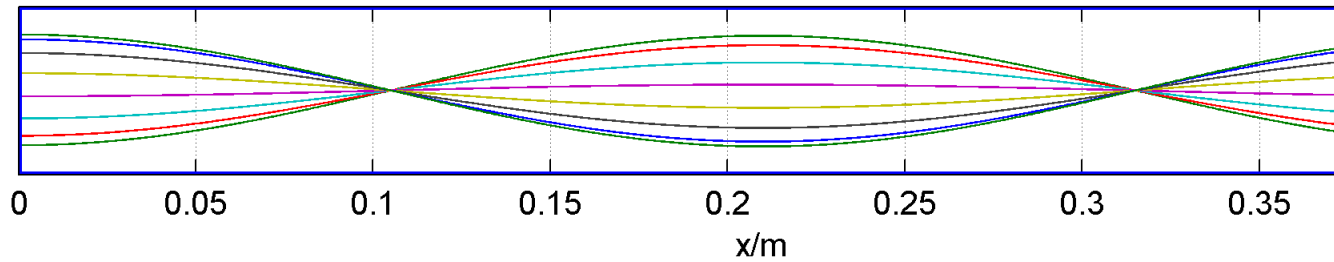


Christopher Cheng (Winchester College) plays an electric cello into a Rubens Tube

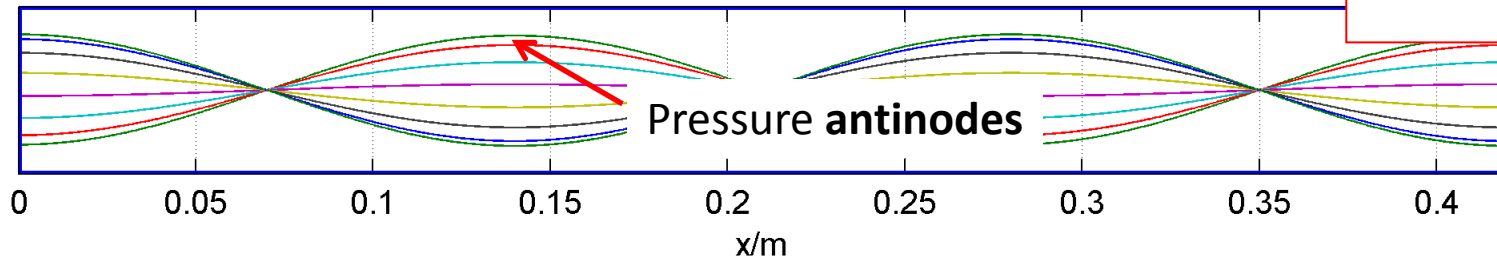
PRESSURE: L = 0.42m, Fundamental frequency = 404.7619Hz,  $\lambda = 0.84\text{m}$



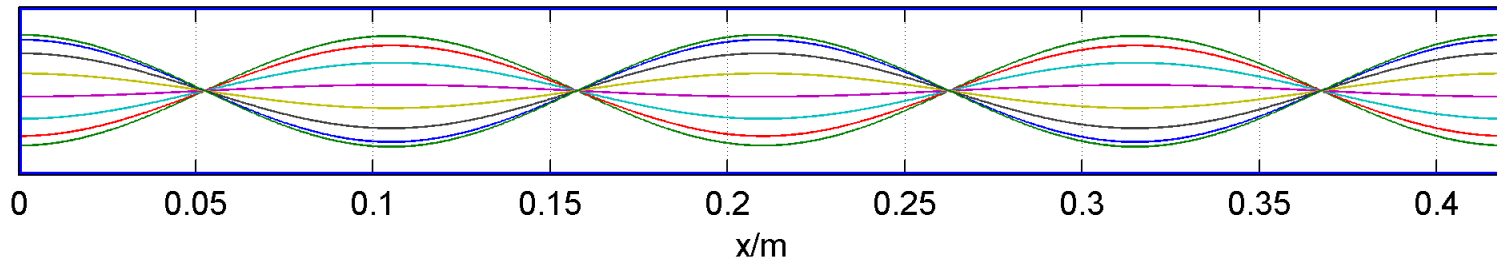
Harmonic #1 frequency = 809.5238Hz,  $\lambda = 0.42\text{m}$



Harmonic #2 frequency = 1214.2857Hz,  $\lambda = 0.28\text{m}$



Harmonic #3 frequency = 1619.0476Hz,  $\lambda = 0.21\text{m}$



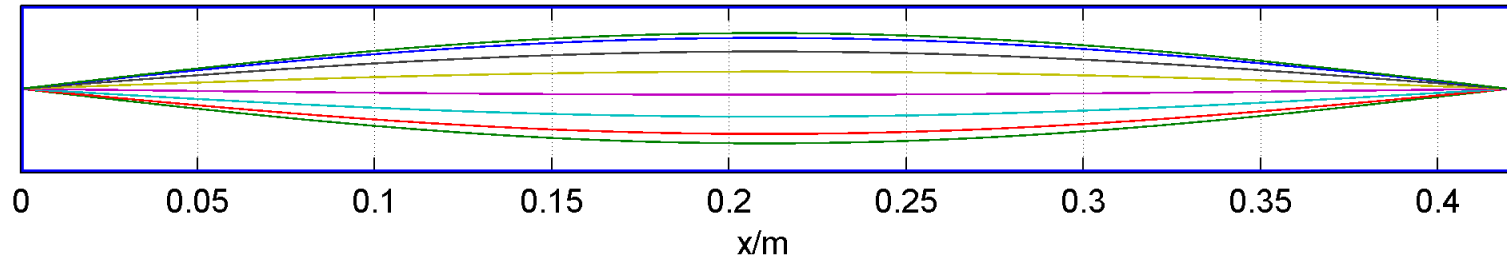
$$f_n = \frac{c}{2L} n$$

$$\lambda_n = \frac{c}{f_n} = \frac{2L}{n}$$

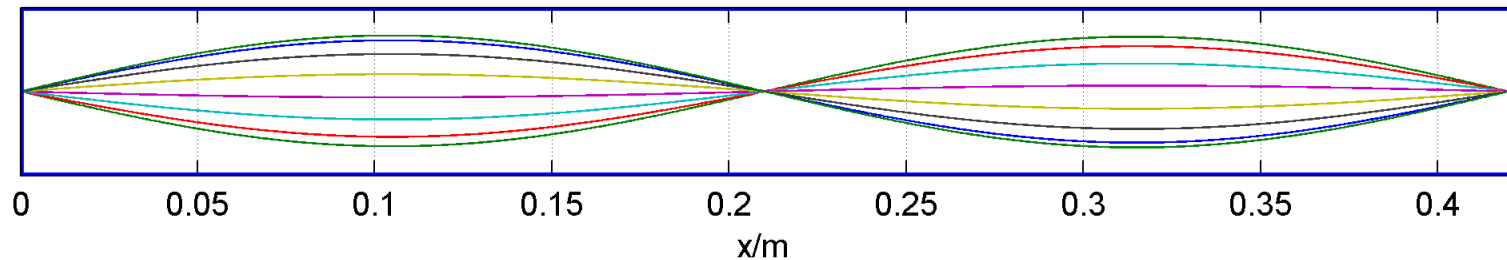
Standing waves in an **closed ended tube**: Air pressure vs distance at times within a wave period



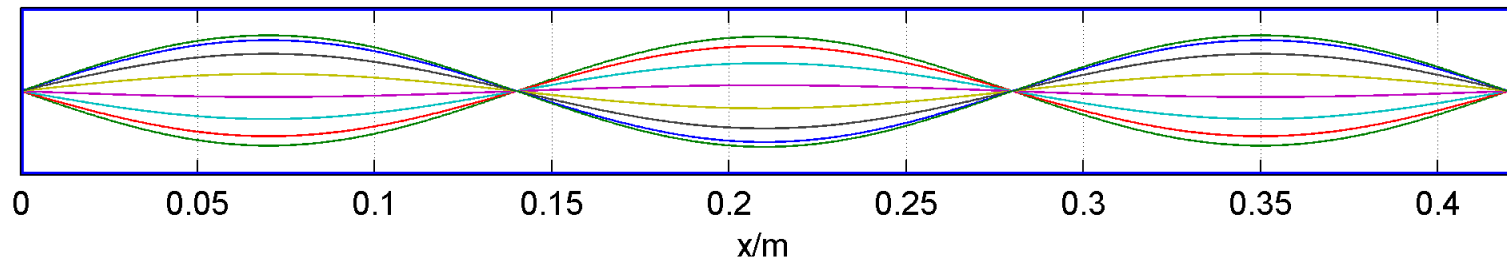
DISPLACEMENT:  $L = 0.42\text{m}$ , Fundamental frequency =  $404.7619\text{Hz}$ ,  $\lambda = 0.84\text{m}$



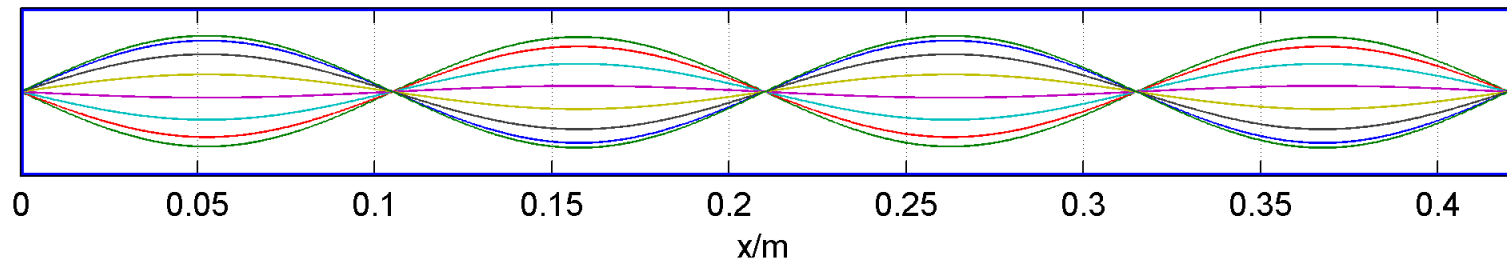
Harmonic #1 frequency =  $809.5238\text{Hz}$ ,  $\lambda = 0.42\text{m}$



Harmonic #2 frequency =  $1214.2857\text{Hz}$ ,  $\lambda = 0.28\text{m}$



Harmonic #3 frequency =  $1619.0476\text{Hz}$ ,  $\lambda = 0.21\text{m}$

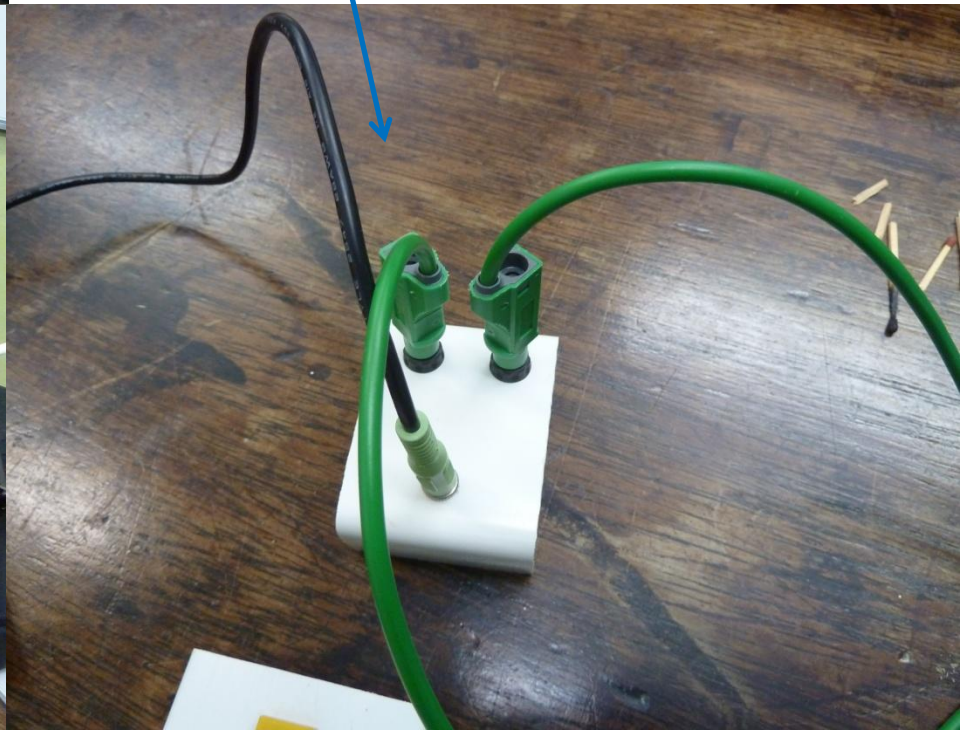


Standing waves in an **closed ended tube**: Air displacement vs distance vs  $t$  within a wave period



Plug an mp3 player or electric guitar into the signal generator amplifier input.

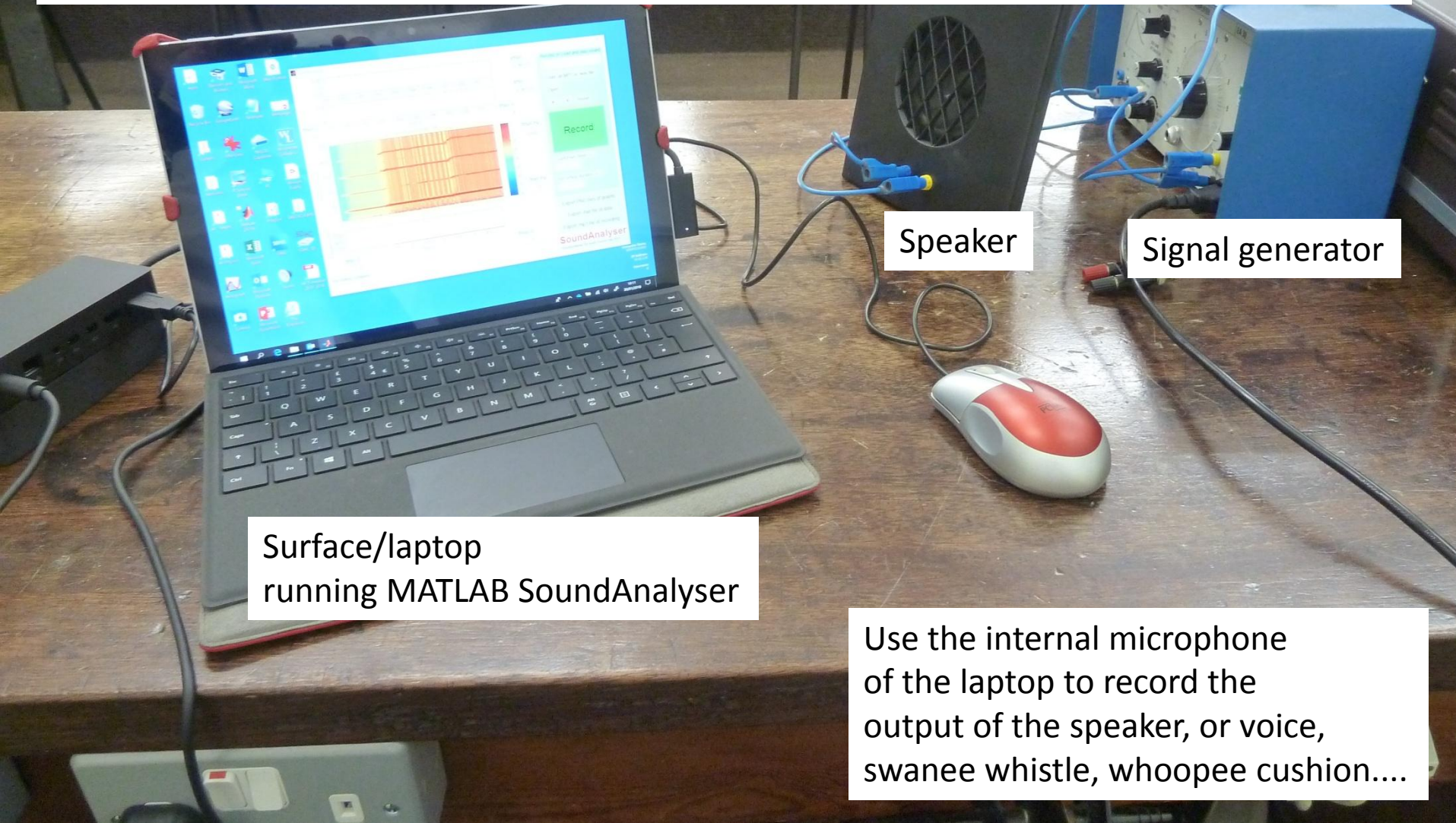
Use the headphone output of the guitar amplifier as an input to the signal generator.





# JP Waves Circus Demonstrations

## #7 Signal generator, oscilloscope & spectrogram via MATLAB SoundAnalyser



Speaker

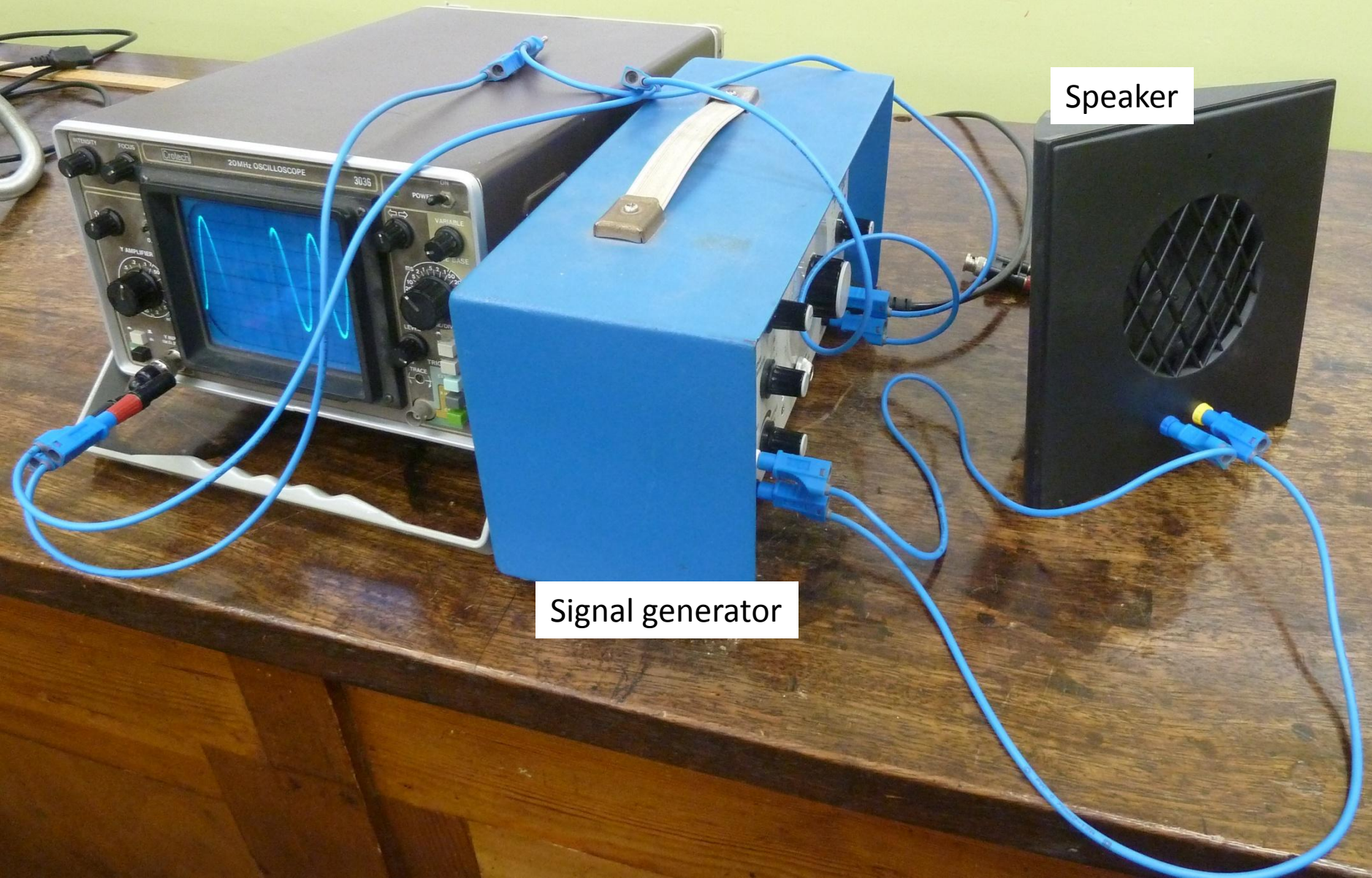
Signal generator

Surface/laptop  
running MATLAB SoundAnalyser

Use the internal microphone  
of the laptop to record the  
output of the speaker, or voice,  
swanee whistle, whoopee cushion....



For a signal generator output, additionally display waveform using an oscilloscope

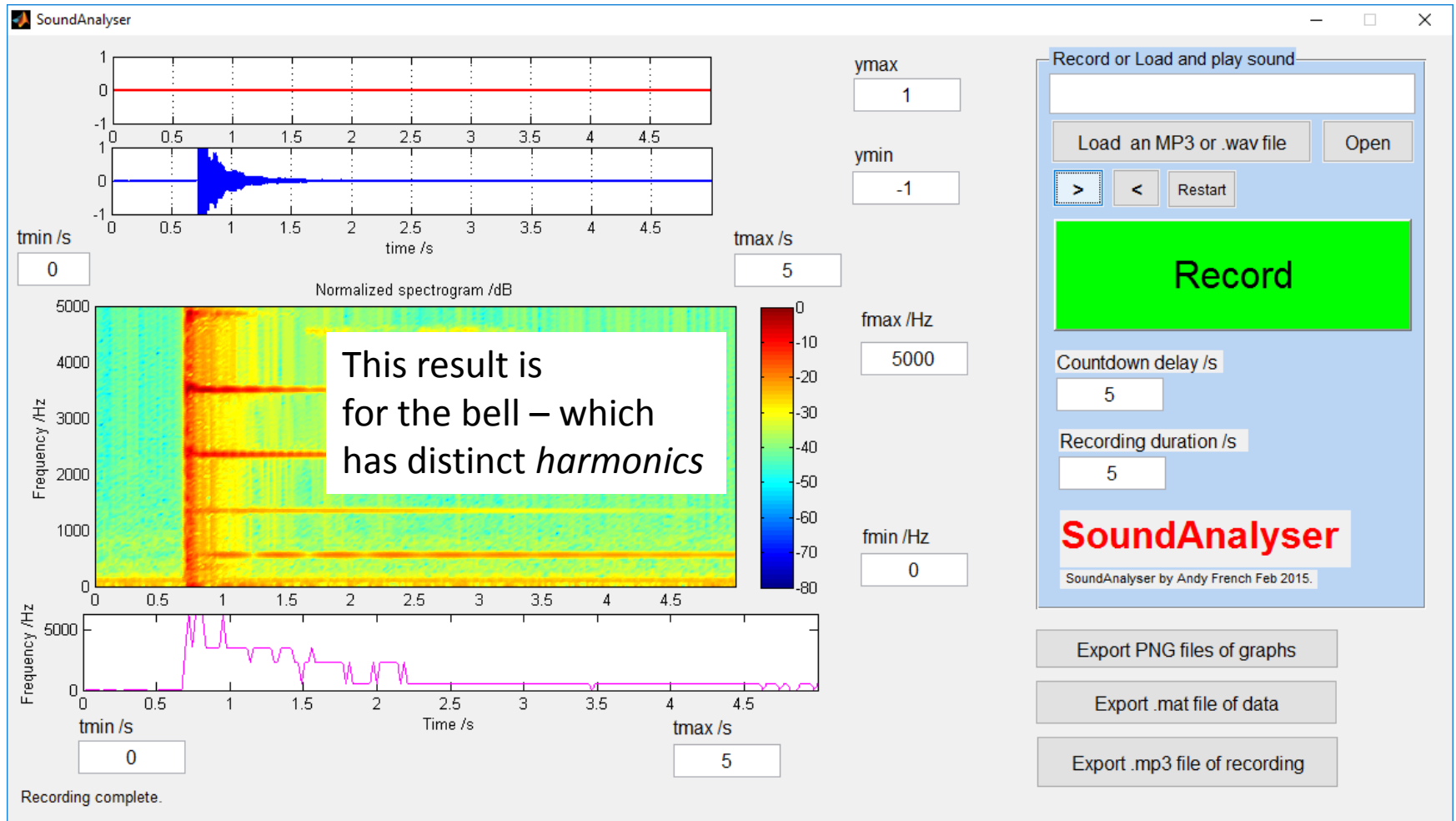


Speaker

Signal generator



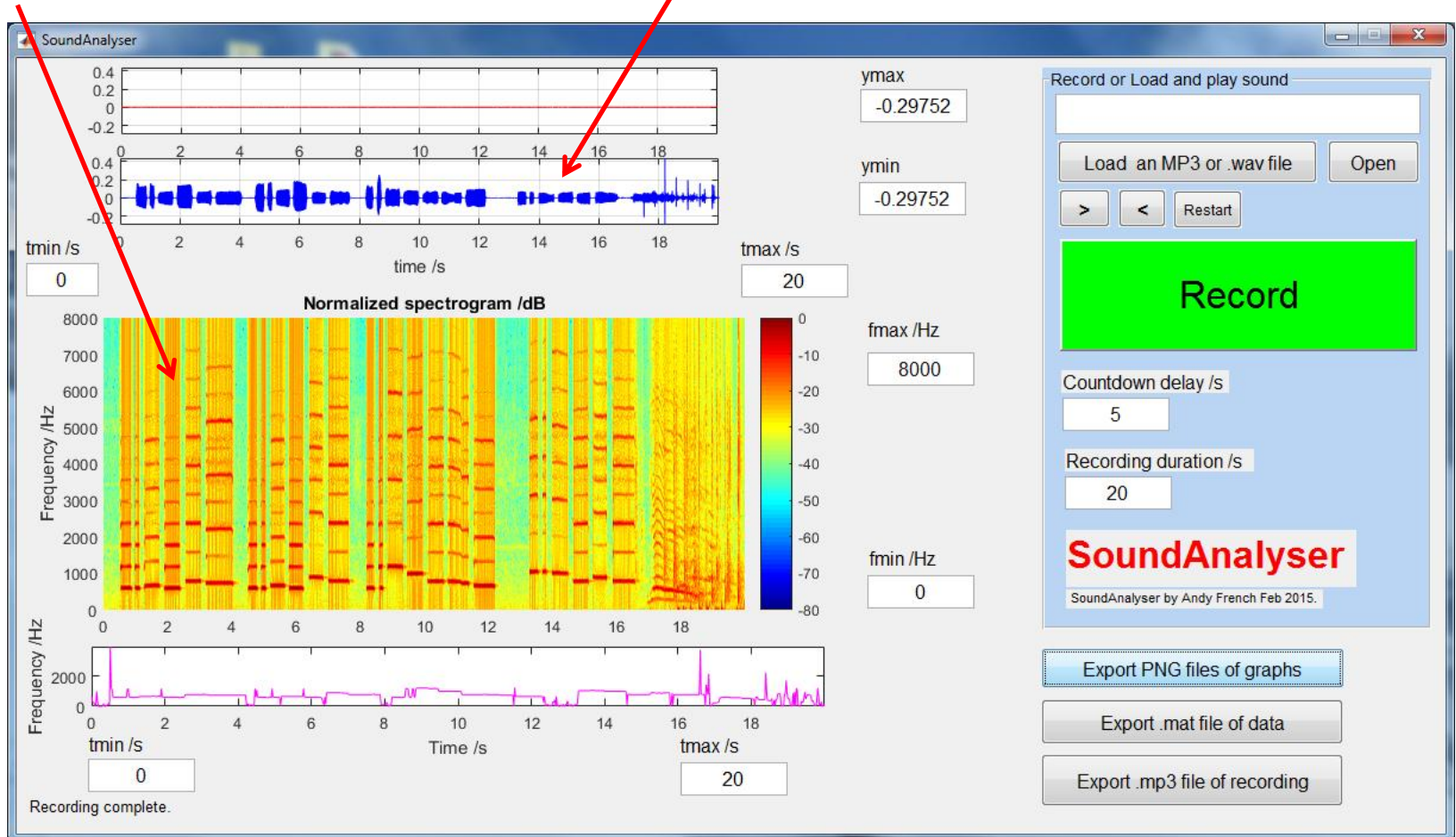
Run **MATLAB** and run **SoundAnalyser.m** within the MATLAB command window. The following GUI will appear.



Pressing **Record** will record sound and then analyse it i.e. amplitude vs time and frequency spectrum vs time (plus 'dominant' frequency vs time) graphs will be generated.

Spectrogram – frequency content vs time

Wave amplitude vs time



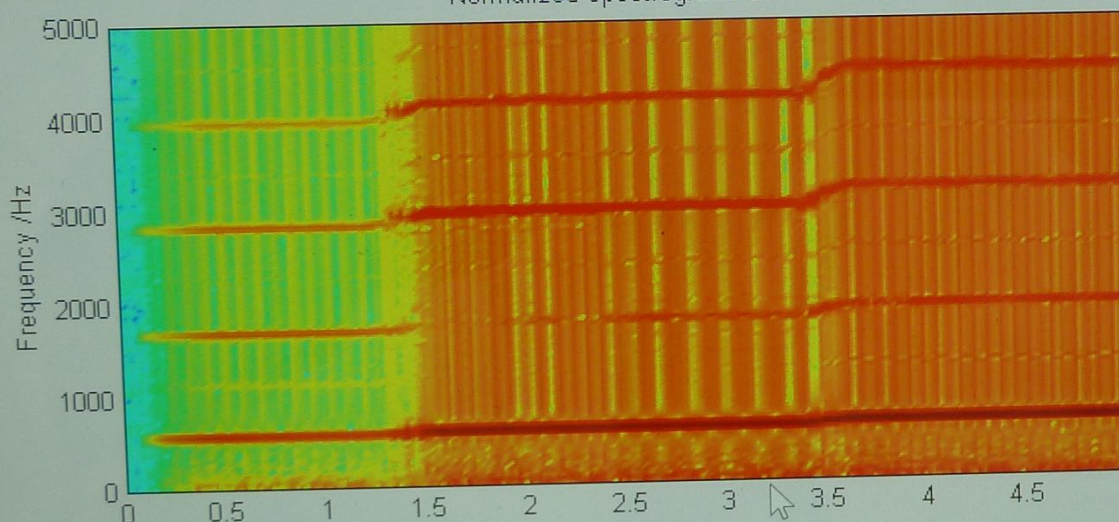
Happy birthday, played by a flute





tmin /s  
3.99

Normalized spectrogram /dB



SoundAnalyser screen shot, recording three tones from the signal generator

ymin  
-0.063751

ymin  
-0.063751

tmax /s  
4

fmax /Hz  
5000

fmin /Hz  
0

tmax /s  
5

Record or Load and play sound

Load an MP3 or .wav file

Open

>

<

Restart

Record

Countdown delay /s

5

Recording duration /s

5

Export PNG files of graphs

Export .mat file of data

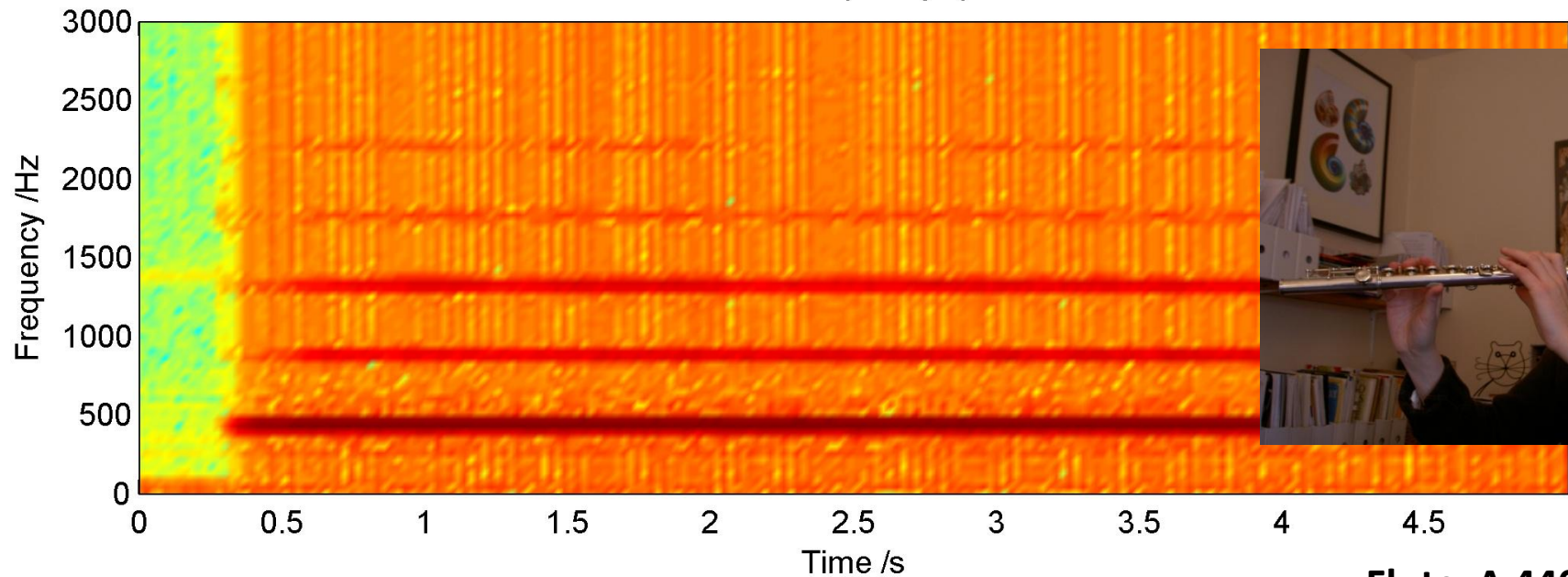
Export .mp3 file of recording

SoundAnalyser

SoundAnalyser by Andy French Feb 2015.

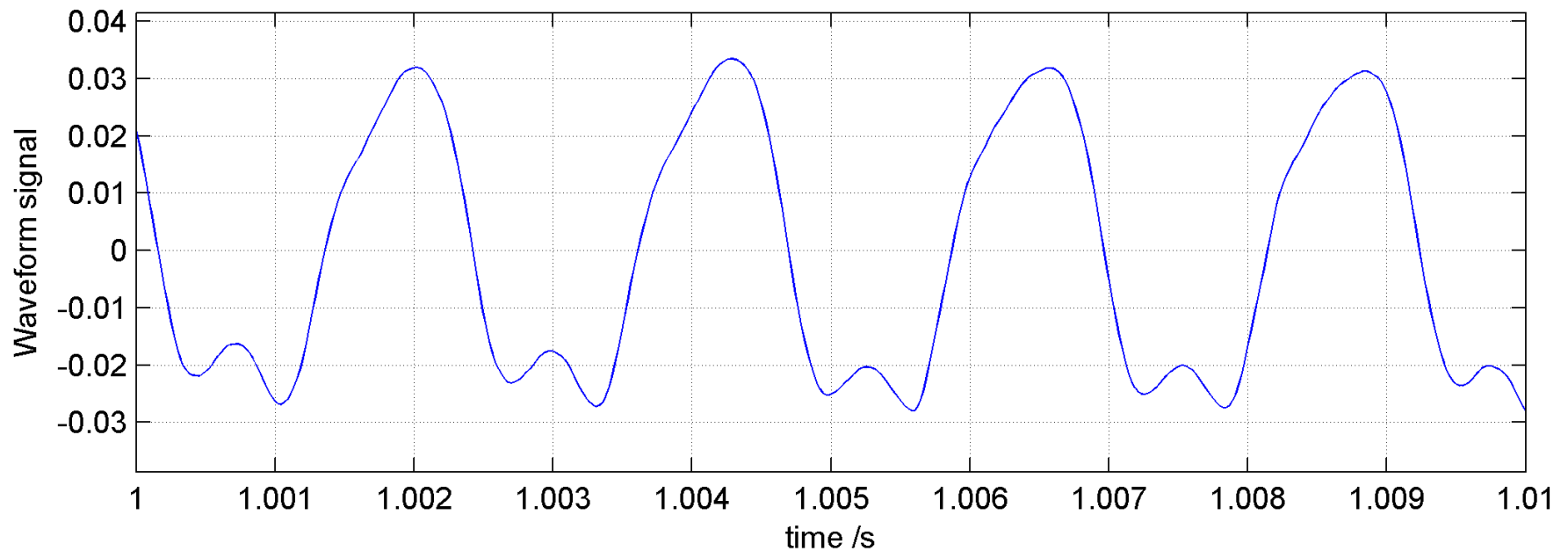
Recording complete.

Frequency spectrum variation with time



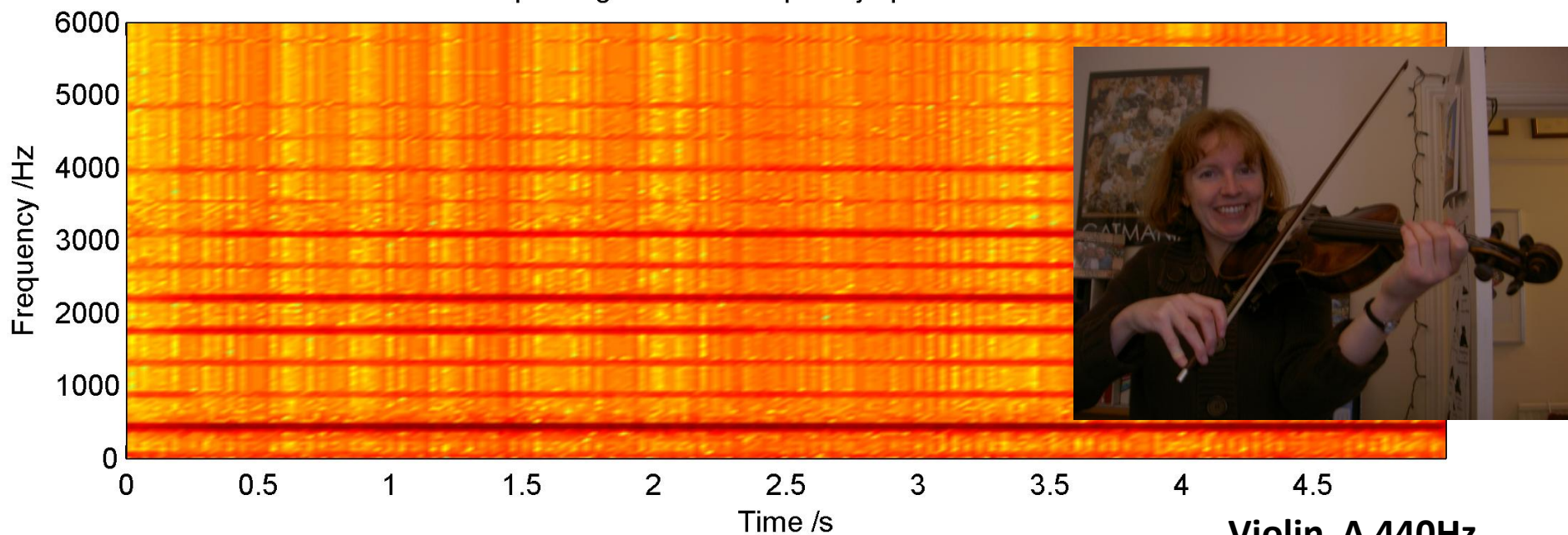
**Flute A 440Hz**

Waveform signal vs time: Right channel

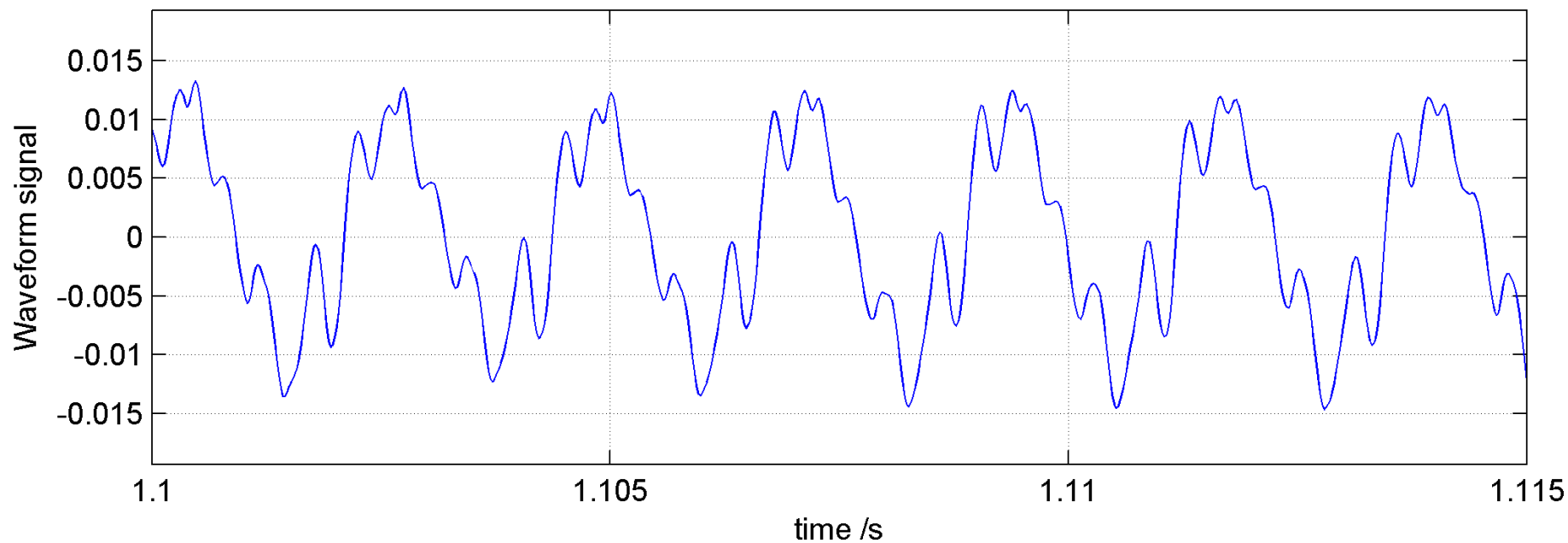




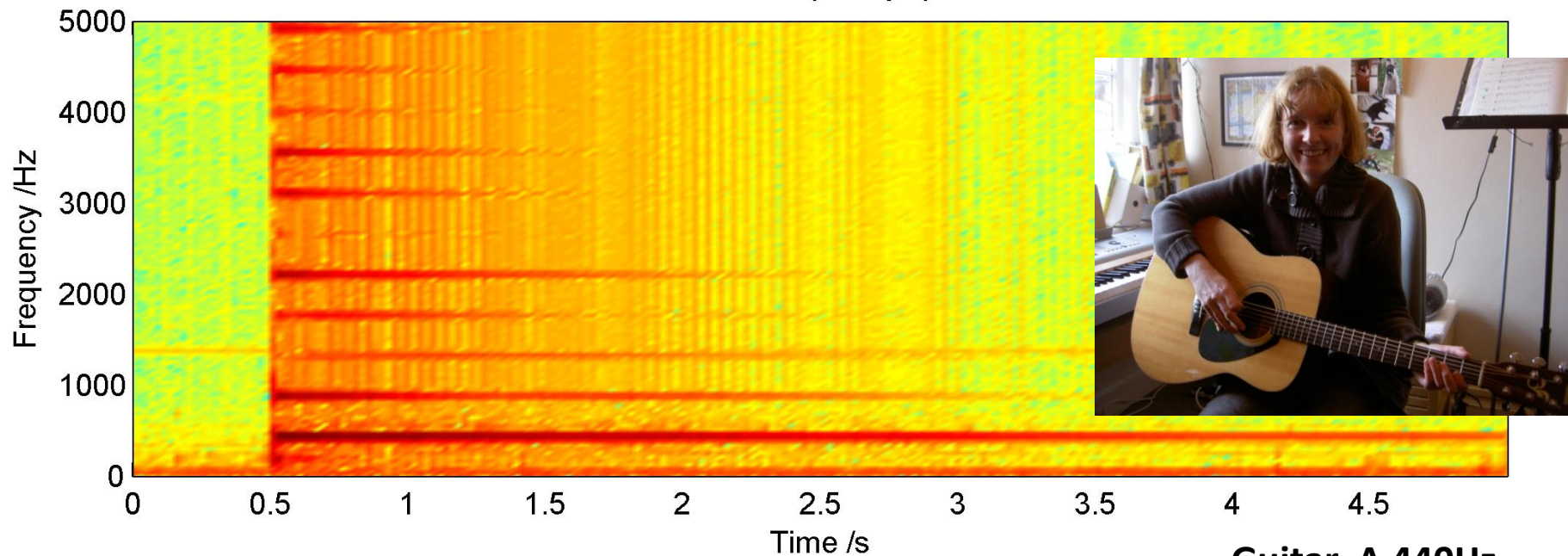
Normalized spectrogram /dB: Frequency spectrum variation with time



Waveform signal vs time: Right channel

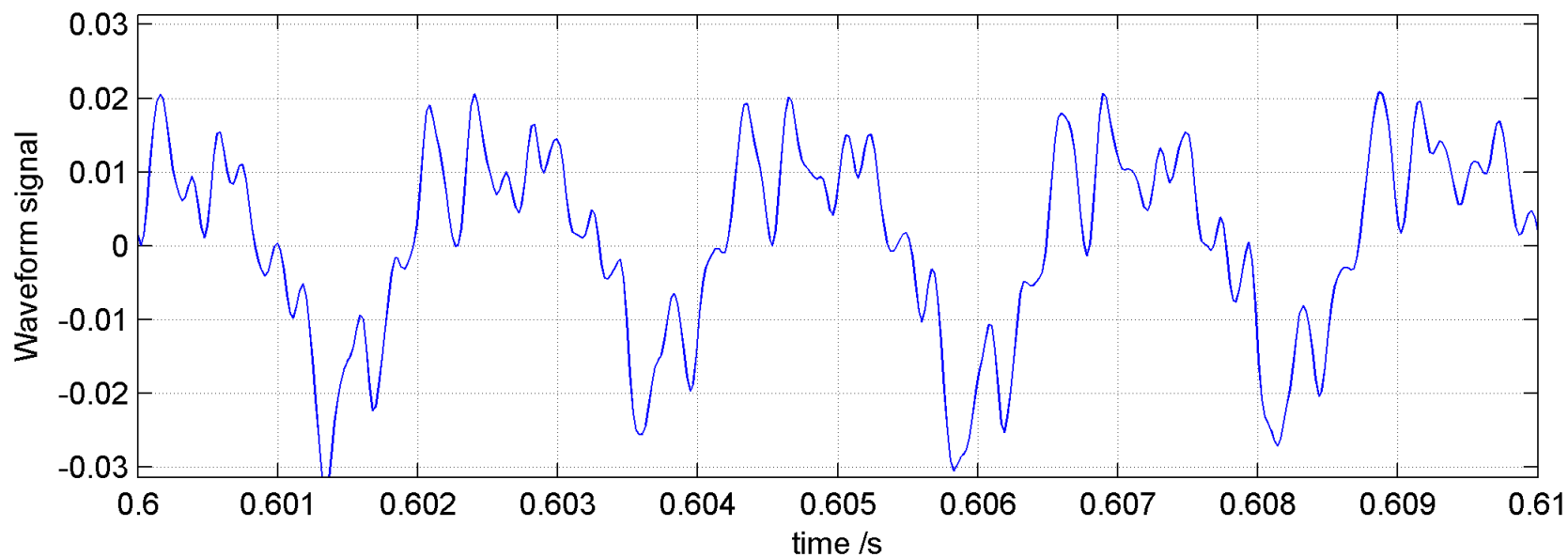


Frequency spectrum variation with time



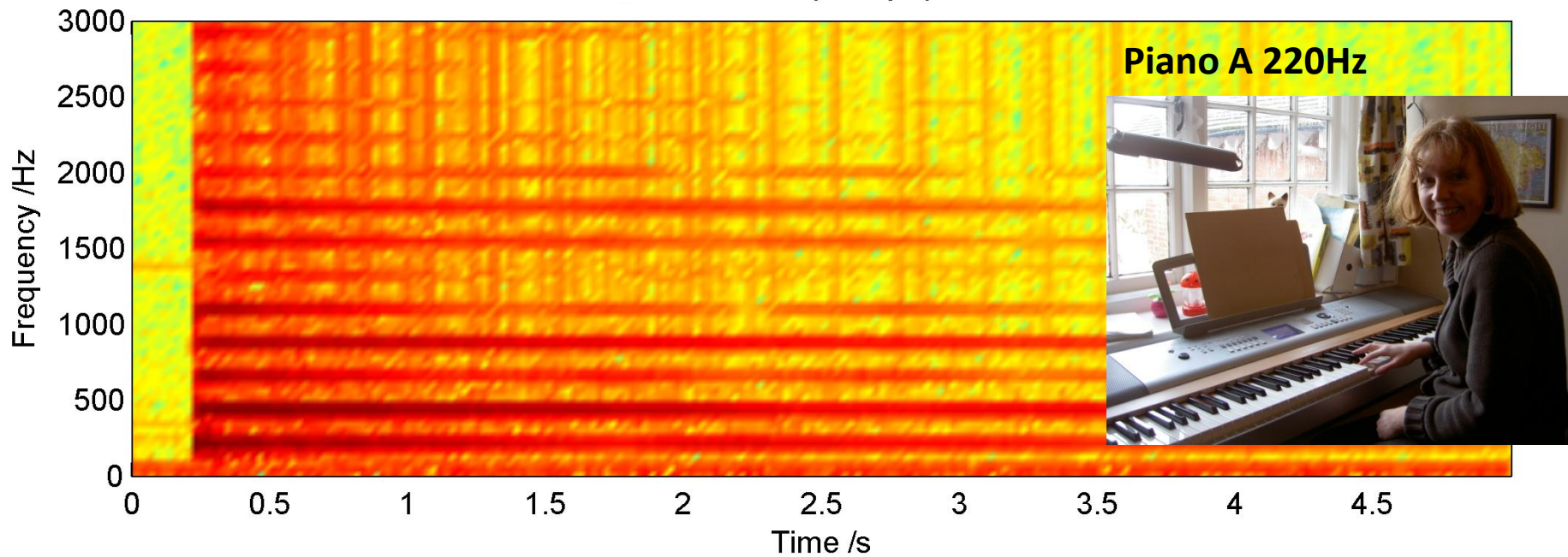
**Guitar A 440Hz**

Waveform signal vs time: Right channel

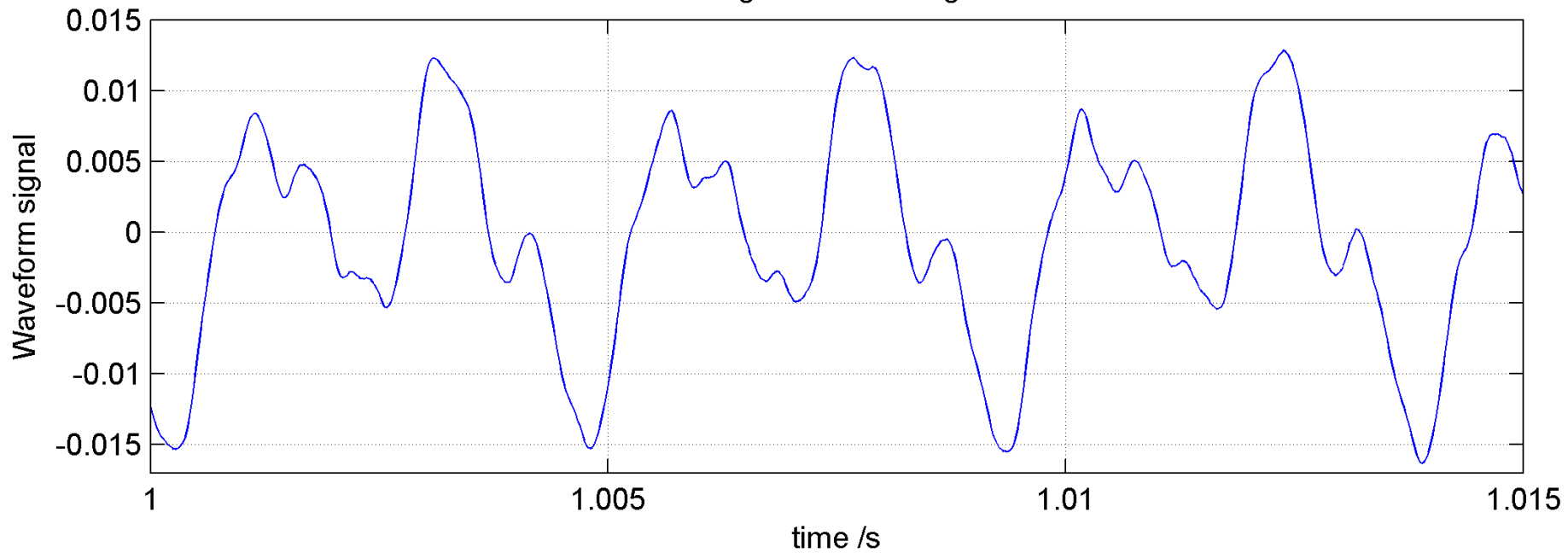




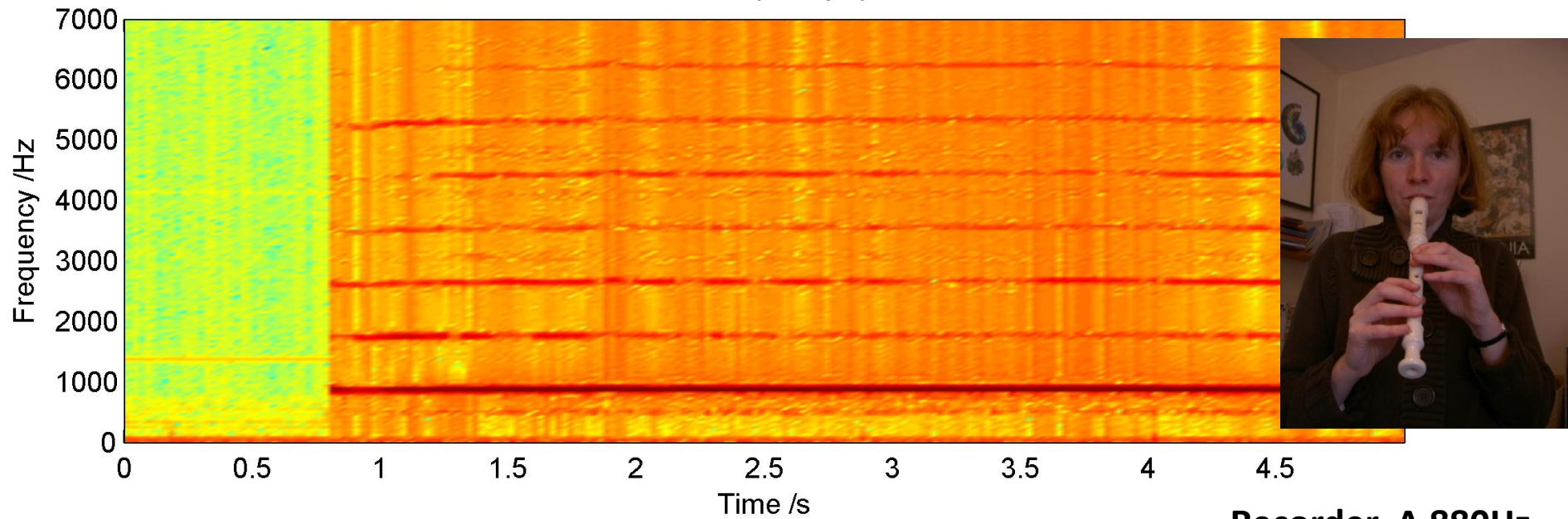
Frequency spectrum variation with time



Waveform signal vs time: Right channel

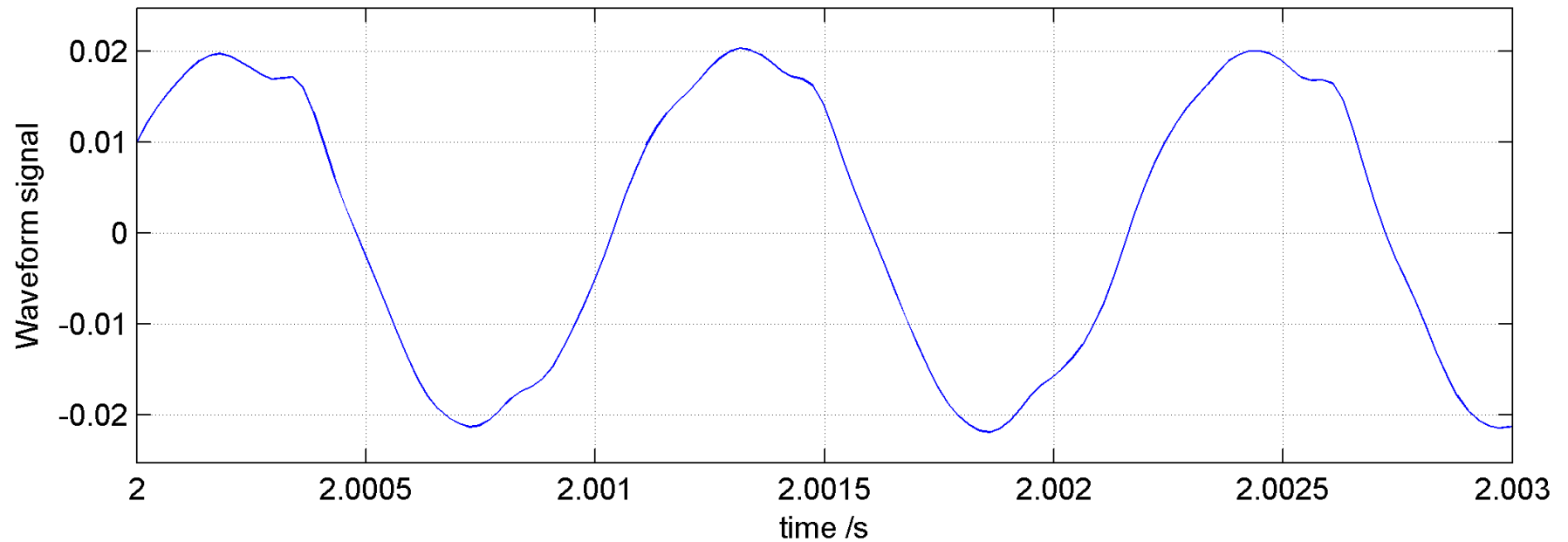


Frequency spectrum variation with time



**Recorder A 880Hz**

Waveform signal vs time: Right channel



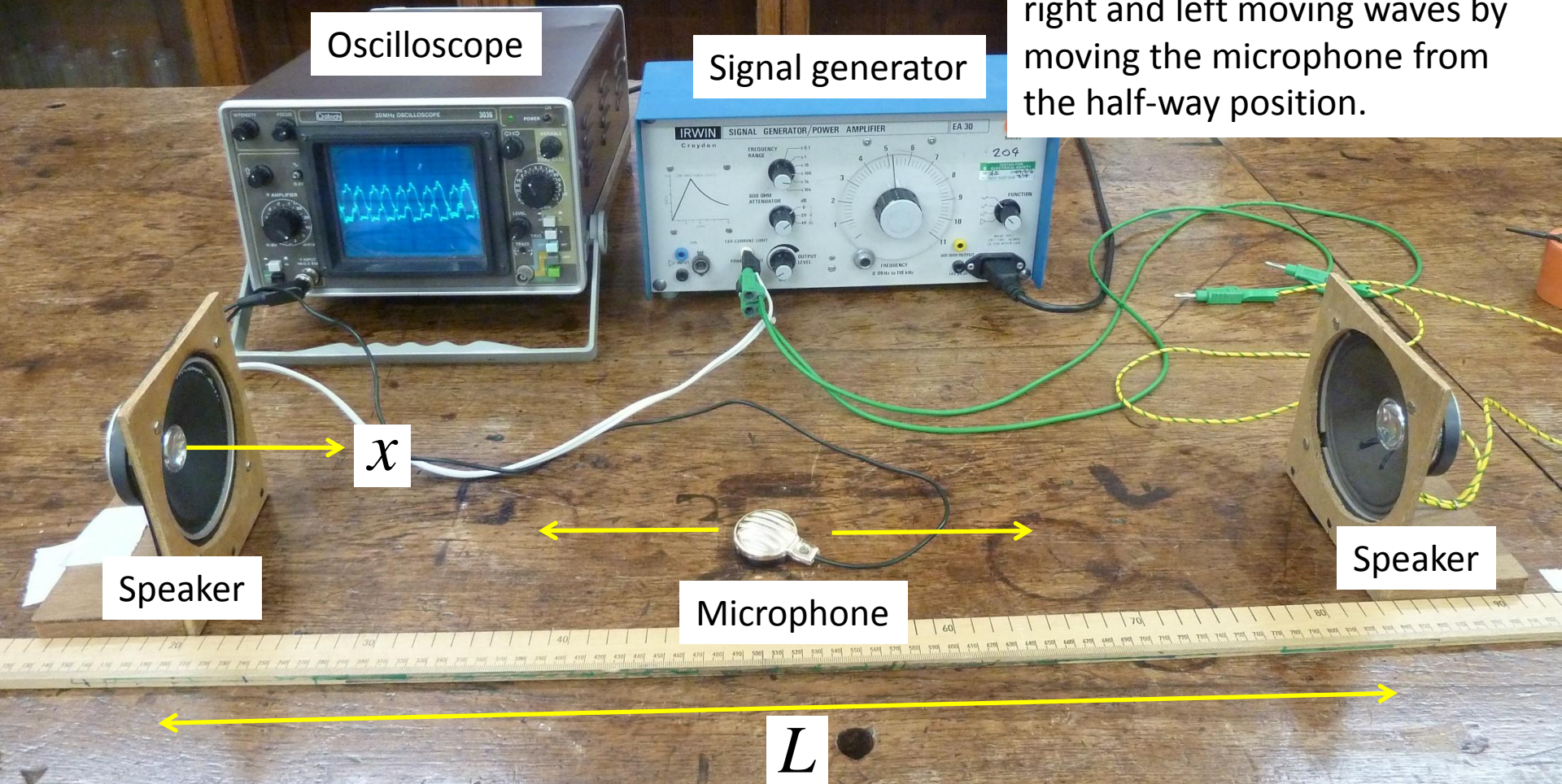


# JP Waves Circus Demonstrations

## #8 Signal generator and two-speaker sound interference

Each opposing speaker is driven by the same output from the signal generator.

Explore the spatial variation of the resulting **standing wave** formed by **interference** of the right and left moving waves by moving the microphone from the half-way position.



Interference of standing waves from speakers separated by distance  $L$

$$\psi = A \cos(kx - \omega t) + A \cos(-k(x - L) - \omega t) \quad \text{Assume waves start in phase!}$$

$$\frac{\psi}{A} = 2 \cos\left(\frac{kx - \omega t - k(x - L) - \omega t}{2}\right) \cos\left(\frac{kx - \omega t + k(x - L) + \omega t}{2}\right)$$

$$\frac{\psi}{A} = 2 \cos\left(\frac{kL - 2\omega t}{2}\right) \cos\left(\frac{2kx - kL}{2}\right)$$

$$\frac{\psi}{A} = 2 \cos\left(\frac{1}{2} kL - \omega t\right) \cos\left(kx - \frac{1}{2} kL\right)$$

$$k = \frac{2\pi}{\lambda}$$

$$\omega = 2\pi f$$

So when  $x = L/2$ , the above equation predicts that there should always be a **maximum**, which oscillates at the frequency of the tone generator

$$\sin A + \sin B = 2 \sin \frac{A+B}{2} \cos \frac{A-B}{2}$$

$$\sin A - \sin B = 2 \cos \frac{A+B}{2} \sin \frac{A-B}{2}$$

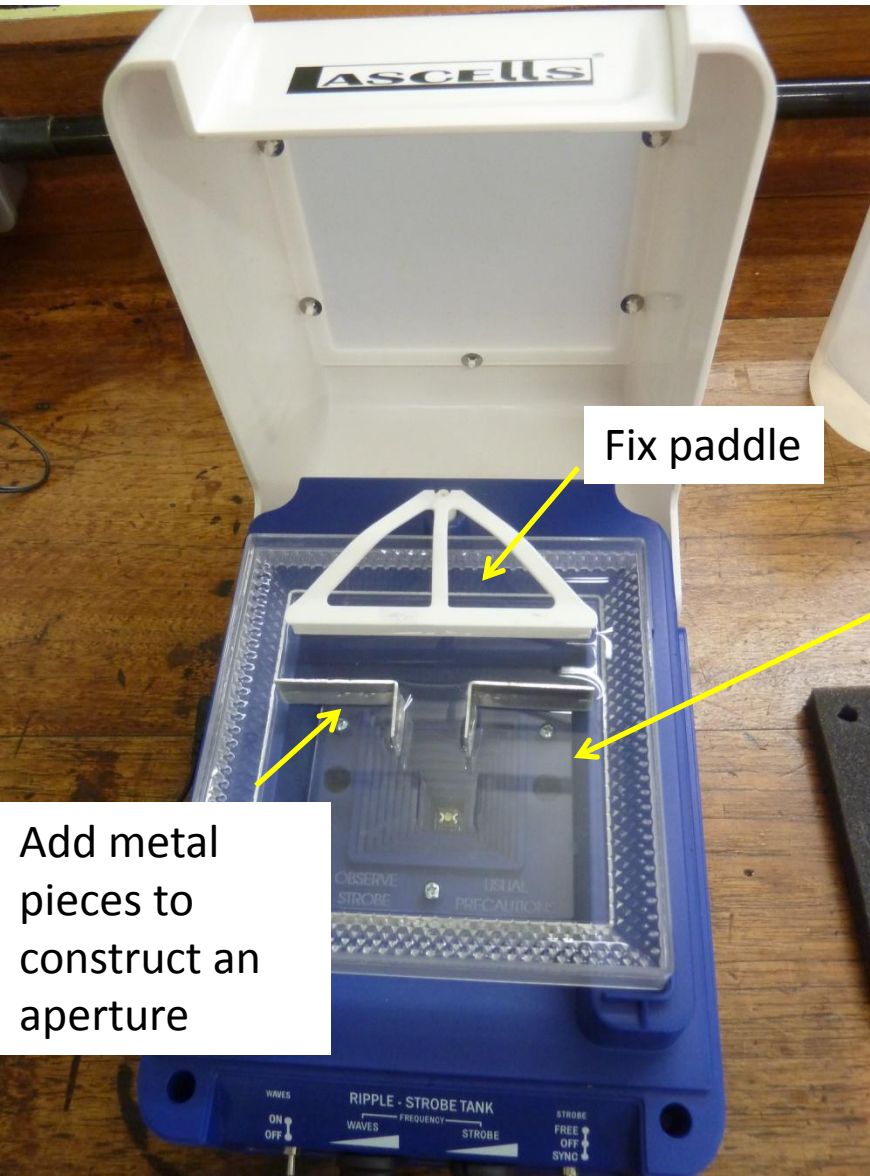
$$\cos A + \cos B = 2 \cos \frac{A+B}{2} \cos \frac{A-B}{2}$$

$$\cos A - \cos B = -2 \sin \frac{A+B}{2} \sin \frac{A-B}{2}$$



# JP Waves Circus Demonstrations

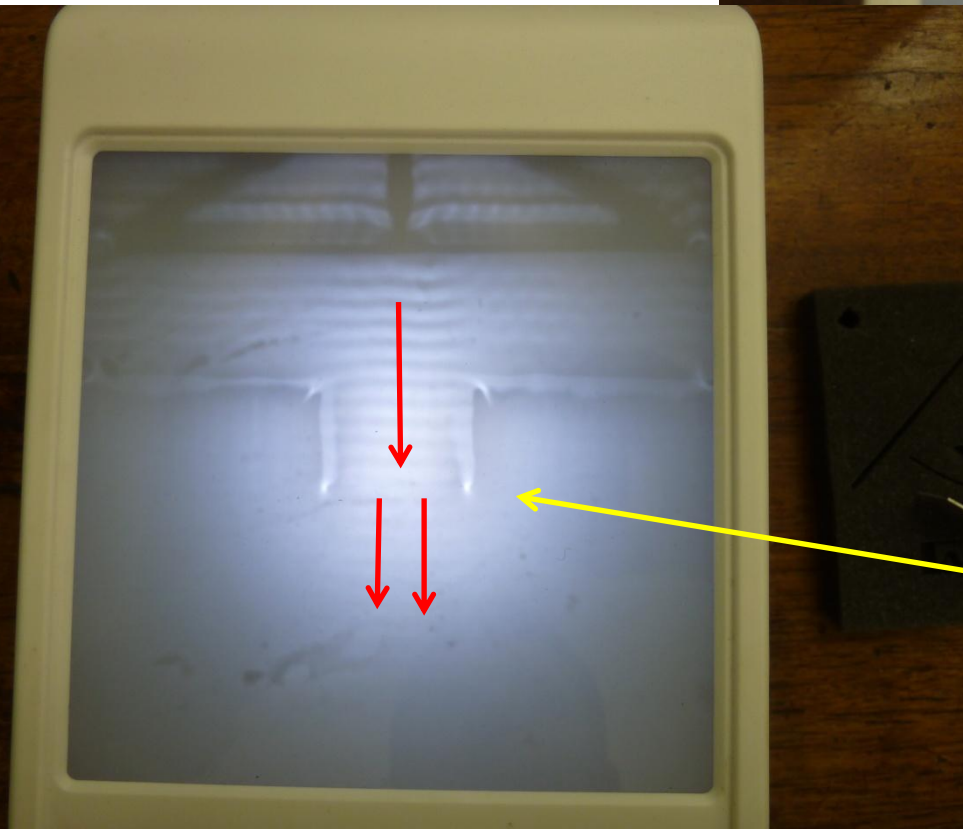
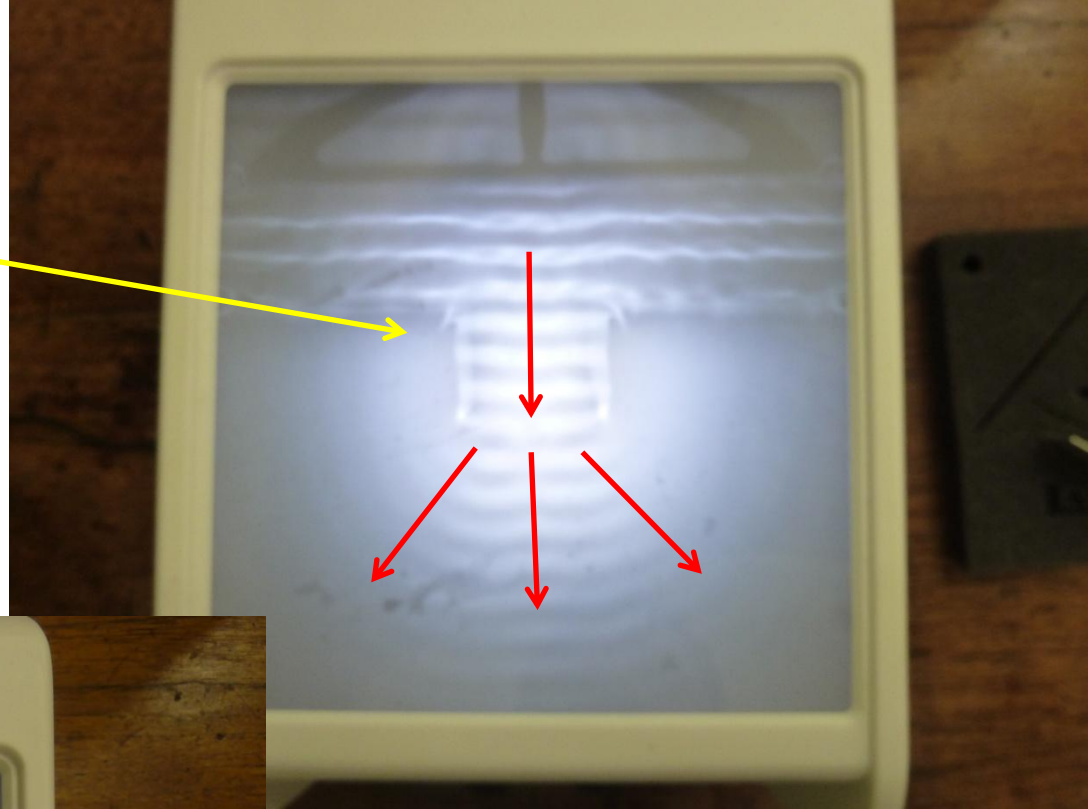
## #9 Diffraction of water waves using a ripple tank



Fill ripple tank tray with distilled water



Increase wavelength  
until it approaches  
the aperture width.  
This results in maximum  
**diffraction**



Reducing the wavelength  
minimizes diffraction effects.  
The wavefronts emerge from the  
aperture without significant  
circular spreading.