

## $10^{9}$ Billion <br>  <br> $10^{12}$ <br> Trillion <br> 100 <br> MI <br>  <br> Andy French

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Here is a millionaire's shortbread 'mini bite' from a supermarket


It has a square cross section of side length 28 mm and it is 12 mm thick.


## A million is a thousand thousand:

$1,000,000=1,000^{2}=\left(10^{3}\right)^{2}=10^{6}=\left(10^{2}\right)^{3}=100 \times 100 \times 100$
So a million millionaire mini bites will be a stack of 100 wide by 100 deep by 100 high.

$$
1 \mathrm{~m}=1,000 \mathrm{~mm} \quad \therefore 1 \mathrm{~mm}=\frac{1}{1,000} \mathrm{~m}
$$

Convert mm to metres (m)
$\therefore 28 \mathrm{~mm} \times 100=28 \times \frac{1}{1,000} \mathrm{~m} \times 100=2.8 \mathrm{~m}$
$\therefore 12 \mathrm{~mm} \times 100=12 \times \frac{1}{1,000} \mathrm{~m} \times 100=1.2 \mathrm{~m}$
... So a million mini-bites will form a cuboid
2.8 m wide, 2.8 m deep and 1.2 m high.


Sybil the cat is $460 \mathrm{~mm}=0.46 \mathrm{~m}$
long. So 2.8 m is just over 6 cats and 1.2 m is 2.6 cats $\frac{2.8}{0.46}=6.1 \quad$ to 2.s.f


## A billion is a thousand million:

$$
\begin{aligned}
& 1,000 \times 1,000,000=10^{9}=\left(10^{3}\right)^{3}=1,000 \times 1,000 \times 1,000 \\
& =(10 \times 100) \times(10 \times 100) \times(10 \times 100)
\end{aligned}
$$

Which means a billion mini-bites form a cuboid which is ten times larger in every dimension than a million mini bites.

Which is about the volume size of a large sports hall or barn.


## An Olympic swimming pool is 50 m long, 25 m wide and up to 3 m deep.

So a billion mini-bites is equivalent to
$\frac{12 \mathrm{~m} \times 28 \mathrm{~m} \times 28 \mathrm{~m}}{50 \mathrm{~m} \times 25 \mathrm{~m} \times 3 \mathrm{~m}}=2.51$

Olympic swimming pools by volume


## A trillion is a thousand billion:

$$
\begin{aligned}
& 1,000 \times 1,000,000,000=10^{12}=\left(10^{4}\right)^{3}=10,000 \times 10,000 \times 10,000 \\
& =(10 \times 10 \times 100) \times(10 \times 10 \times 100) \times(10 \times 10 \times 100)
\end{aligned}
$$

Which means a trillion mini-bites form a cuboid which is ten times larger in every dimension than a billion mini-bites.

The Titanic was 269 m long, so would nearly form one edge of the trillion mini-bite cross section.


What does a trillion pounds look like? (Note the Gross Domestic Product (GDP) of the UK is about 2.2 trillion, and the total tax income to the UK is about 0.9 trillion per year)
.$\longleftarrow \underline{2020-2021 \text { figures }}$

A $£ 1$ coin has a volume of:

$$
\begin{aligned}
& \pi \times\left(\frac{1}{2} \times 23.43 \mathrm{~mm}\right)^{2} \times 2.8 \mathrm{~mm}=1,207 \mathrm{~mm}^{3} \\
& =1,207 \times\left(\frac{1}{1,000} \mathrm{~m}\right)^{3} \\
& =1.207 \times 10^{-6} \mathrm{~m}^{3}
\end{aligned}
$$

So a trillion pounds has a volume of:

$$
\begin{aligned}
& 10^{12} \times 1.207 \times 10^{-6} \mathrm{~m}^{3}=1.207 \times 10^{6} \mathrm{~m}^{3} \\
& =1.207 \mathrm{~m} \times 1000 \mathrm{~m} \times 1000 \mathrm{~m}
\end{aligned}
$$

i.e. a square kilometre of pound


Note a cubic metre has $1,000^{3}=1$ billion cubic $\mathbf{m m}$. coins that are 1.207 m deep. A kilometre is $10 \times 100 \mathrm{~m}$ running track straights laid end to end.

$$
\pi=3.141592654 \ldots
$$

A $£ 1$ coin has a mass of 8.75 g so a trillion pounds has a mass of:

$$
10^{12} \times 8.75 \times 10^{-3} \mathrm{~kg}=8.75 \times 10^{9} \mathrm{~kg}
$$

i.e. 8.75 billion kg or 8.75 million metric tonnes
(a metric tonne is $1,000 \mathrm{~kg}$ )

Note the Titanic had a mass of: $46,000,000 \mathrm{~kg}=4.6 \times 10^{7} \mathrm{~kg}$

So a trillion $£ 1$ coins has a mass equivalent to 190 Titanics.
$\frac{8.75 \times 10^{9}}{4.6 \times 10^{7}} \approx 190$

## Other visualizations:

## BBC What dos a billion pounds look like?

WIRED What Apple's cash (\$250
billion) looks like

