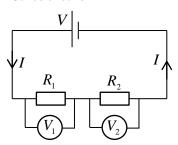
### Series & Parallel circuits

Electronic systems consist of networks of basic components which modify the rate of flow of charge (current) and energy per unit charge (voltage) between two points in the network. In order to model the behaviour of a system, it is useful to understand the basic mathematical features. We shall consider resistive components and the difference between series and parallel arrangements of resistors. Ohmic components are those which have a constant resistance.

## Series circuits



The same current must flow through every component in the loop, otherwise charge would be created or lost.

 $V_1 = IR_1$  $V_2 = IR_2$ 

Apply 'V=IR' to each resistor in turn

V = IR

Apply 'V=IR' to entire series loop.

R is the total resistance

 $V = V_1 + V_2$ 

The applied voltage *V* must be divided across the resistors

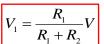
Hence:

$$IR = IR_1 + IR_2$$

so series resistors add

We can use this result to show that resistances in series can act as potential dividers

$$I = \frac{V_1}{R_1} = \frac{V}{R}$$
  $\therefore \frac{V_1}{R_1} = \frac{V}{R_1 + R_2}$ 



 $V_1 = \frac{R_1}{R_1 + R_2} V$  i.e. the voltage across a resistor is the same fraction of the applied voltage as the ratio of resistance to the total resistance.

## Definition of resistance

V = IR <Resistance /ohms  $(\Omega)$ Energy per unit charge

Current / amps Rate of flow of charge through resistor R

Note due to a quirk of history, conventional current is the 'flow of positive charge'. Unfortunately electrons were discovered after many of the electrical conventions were fixed. Since it is the electrons which are mobile in a conductor, current can be thought of as the flow of 'holes' of net positive charge left when an electron has been moved via an electric field.



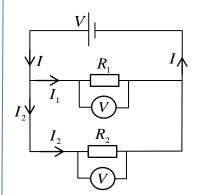
Georg Ohm 1789-1854

## Parallel circuits

Voltage / volts

of resistance R

lost across a conductor



V = IRApply 'V=IR' to entire circuit. R is the total resistance

Apply 'V=IR' to each resistor in turn. Same electric field across  $V = I_1 R_1$ each loop, so the same voltage is dropped across the  $V = I_2 R_2$  resistors

Current is assumed to be contained within the circuit, hence:

Therefore:

$$V/R = V/R_1 + V/R_2$$

$$\therefore \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$$

so parallel resistor loop resistance reciprocals add

Parallel circuit example

 $I_1 = 5/2 = 2.5 \text{mA}$ 

I = voltage / resistance then add currents

 $I_2 = 5/4 = 1.25 \text{mA}$ 

 $I = I_1 + I_2 = 3.75 \text{mA}$ 

Or alternatively ...

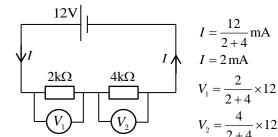
$$\frac{\frac{1}{2} + \frac{1}{4}}{I = 5 / \frac{4}{3} = \frac{15}{4} \text{ mA}} = 3.75 \text{ mA}$$

Use reciprocal resistance addition rule

# Series circuit example



Gustav Kirchhoff 1824-1887



$$I = 2 \text{ mA}$$

$$V_{1} = \frac{2}{2+4} \times 12 = \boxed{4V}$$

$$V_{2} = \frac{4}{2+4} \times 12 = \boxed{8V}$$

$$I = I_{1} + I_{2} = \boxed{3.75 \text{ m}}$$

$$R = \frac{1}{\frac{1}{2} + \frac{1}{4}} = \frac{4}{3} \text{ k}\Omega$$

$$I = 5 / \frac{4}{3} = \frac{15}{4} \text{ mA} = \boxed{1}$$